ThunderRW: An In-Memory Graph Random Walk Engine

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ABSTRACT

As random walk is a powerful tool in many graph processing, mining and learning applications, this paper proposes an efficient inmemory random walk engine named ThunderRW. Compared with existing parallel systems on improving the performance of a single graph operation, ThunderRW supports massive parallel random walks. The core design of ThunderRW is motivated by our profiling results: common RW algorithms have as high as 73.1% CPU pipeline slots stalled due to irregular memory access, which suffers significantly more memory stalls than the conventional graph workloads such as BFS and SSSP. To improve the memory efficiency, we first design a generic step-centric programming model named Gather-Move-Update to abstract different RW algorithms. Based on the programming model, we develop the step interleaving technique to hide memory access latency by switching the executions of different random walk queries. In our experiments, we use four representative RW algorithms including PPR, DeepWalk, Node2Vec and MetaPath to demonstrate the efficiency and programming flexibility of ThunderRW. Experimental results show that ThunderRW outperforms state-of-the-art approaches by an order of magnitude, and the step interleaving technique significantly reduces the CPU pipeline stall from 73.1% to 15.0%.

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The source code of this research paper has been made publicly available at https://github.com/Xtra-Computing/ThunderRW.

1 INTRODUCTION

Random walk (RW) is an effective tool for extracting relationships between entities in a graph, and is widely used in many applications such as *Personalized PageRank* (PPR) [45], *SimRank* [20], *Random Walk Domination* [31], *Graphlet Concentration* (GC) [48], *Network Community Profiling* (NCP) [12], *DeepWalk* [47] and *Node2Vec* [16]. For graph analysis tasks such as GC and NCP, RW queries generally

	<u> </u>
In	put: a graph G and a set \mathbb{Q} of random walk queries;
01	utput: the walk sequences of each query in \mathbb{Q} ;
1 fo	reach $Q \in \mathbb{Q}$ do
2	do
3	Select a neighbor of the current residing vertex Q.cur at random;
4	Add the selected vertex to Q ;
5	while Terminate(Q) is false;
6 re	turn Q;
dom	inate the cost [12, 48]. Even for graph representation learning,
the c	cost of sampling RW is non-trivial, for example, a naive imple-
men	tation of Node2Vec takes more than eight hours on the <i>twitter</i>

Algorithm 1: Execution Paradigm of RW algorithms

the cost of sampling RW is non-trivial, for example, a naive implementation of Node2Vec takes more than eight hours on the *twitter* graph in our experiments. Moreover, increasing the number of RW queries can improve the effectiveness of RW algorithms [16, 48]. Therefore, accelerating RW queries is an important problem.

RW algorithms generally follow the execution paradigm illustrated in Algorithm 1, which consists of massive RW queries. Each query Q starts from a given source vertex. At each step, Q moves to a neighbour of the current residing vertex at random, and repeats this process until satisfying a specific termination condition, e.g., a target length is reached (Lines 2-5). Despite that RW algorithms follow a similar execution paradigm, there are quite some variants of RW algorithms, which can differ significantly in neighbor selections (see Section 2.2). Encouraged by the success of in-memory graph processing engines [44, 55, 58, 68], there have been some recent systems designed specifically for RW algorithms, including C-SAW [46], GraphWalker [60] and KnightKing [66]. They focus on accelerators, disk-based or distributed settings, without specially optimizing in-memory execution of RW queries. However, with the rapid development of hardwares, modern servers equip with hundred gigabytes, even several terabytes memory, which empowers in-memory processing of graphs with hundred billions of edges. This covers many real-world graphs in applications [9]. As such, this paper studies the design and implementation of an in-memory graph engine for RW algorithms.

To crystallize the performance factors for in-memory RW executions, we conduct profiling studies on RW algorithms in comparison with conventional workloads of a single graph operation like BFS and SSSP (see Section 3). Our profiling results show that common RW algorithms have as high as 73.1% CPU pipeline slots stalled due to irregular memory access, which suffers significantly more memory stalls than the conventional workloads. Consequently, the CPUs frequently wait on the high-latency access to the main memory, which becomes the major performance bottleneck. Besides, we observe that the sampling methods such as *inverse transformation sampling* [40], *alias sampling* [59] and *rejection sampling* [50]

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have significant varying performance on different RW algorithms (with the difference as much as 6 times). Thus, it requires nontrivial and significant engineering efforts to develop any efficient RW algorithms considering the cache stall bottleneck, as well as parallelization and the choice of sampling methods.

In this paper, we propose ThunderRW, a generic and efficient in-memory RW framework. We employ a step-centric programming model abstracting the computation from the local view of moving one step of a walker. Users implement their RW algorithms by "thinking like a walker" in user-defined functions (UDF). The framework applies UDFs to each query and parallelizes the execution by regarding a step of a query as a task unit. Furthermore, ThunderRW provides variant sampling methods so that users can select an appropriate one based on the characteristics of workloads. Built upon the step-centric programming model, we propose the step interleaving technique to resolve the cache stalls caused by irregular memory access with software prefetching [29]. As modern CPUs can process multiple memory access requests simultaneously [64], the core idea of step interleaving is to hide memory access latency by issuing multiple outstanding memory accesses, which exploits memory level parallelism [2] among different RW queries.

We demonstrate the generality and programming flexibility of ThunderRW by showcasing four representative algorithms including PPR [45], DeepWalk [47], Node2Vec [16] and MetaPath [57]. We conduct extensive experiments with twelve real-world graphs. The results show that (1) ThunderRW runs 8.6-3333.1X faster than the naive implementation in popular open-source packages; (2) ThunderRW provides speedups of 1.7-14.6X over the state-of-the-art frameworks including GraphWalker [60] and KnightKing [66] running on the same machine; and (3) the step interleaving technique significantly reduces the memory stalls from 73.1% to 15.0%.

2 BACKGROUND AND RELATED WORK

2.1 Preliminary

This paper focuses on the directed graph G = (V, E) where V is a set of vertices and *E* is a set of edges. An undirected graph can be supported by representing each undirected edge with two directed edges with the same two vertexes in our system. Given a vertex $v \in V$, N_v denotes the neighbors of v, i.e., $\{v' | e(v, v') \in E\}$ where e(v, v') represents the edge between v and v'. The degree d_v denotes the number of neighbors of v. E_v is the set of edges adjacent to v, i.e., $\{e(v, v')|v' \in N_v\}$. Given $e \in E$ (resp. $v \in V$), w_e and l_e (resp. w_v and $l_{\boldsymbol{v}})$ represent its weight and label, respectively. Given G, a RW Q is a stochastic process on G, which consists of a sequence of adjacent vertices. Q[i] is the *i*th vertex in the sequence where *i* starts from 0. Q.cur is the current residing vertex of Q. |Q| is the number of vertices in Q. Suppose that Q.cur is v. Given $e \in E_v$, we call the probability of *e* being selected the *transition probability*, which is represented by p(e). Then, the neighbor selection is equivalent to sampling from the discrete probability distribution $P = \{p(e)\}$ where $e \in E_v$. Specifically, it is to pick an element *h* from E_v based on the distribution of P, i.e., P[h = e] = p(e). For example, if the relative chance of e being selected is proportional to the edge weight w_e , then $p(e) = \hat{w}_e$ is the normalized probability where $\hat{w}_e = \frac{w_e}{\sum_{e' \in E_v} w_{e'}}$.

2.2 Random Walk based Algorithms

RW algorithms generally follow the execution paradigm in Algorithm 1. They mainly differ in the neighbor selection step. We first categorize them into *unbiased* and *biased* based on the transition probability properties. Unbiased RW selects each edge $e \in E_v$ with the same probability where v = Q.cur, while the transition probability is nonuniform for biased RWs, e.g., depending on the edge weight. We further classify the biased RWs into *static* and *dynamic*. If the transition probability is determined before execution, then RW is static. Otherwise, it is dynamic, which is affected by states of RW queries. In the following, we introduce four representative RW algorithms that have been used in many applications.

PPR (Personalized PageRank) [45] assigns a score to each vertex v' in the graph from the personalized view of a given source v, which describes how much v is interested in (or similar to) v'. A common solution for this problem is to start a number of RW queries from v, which have a fixed termination probability at each step, and approximately calculates the scores based on the distribution of the end vertices of random walk queries [11, 33]. The algorithms generally set RW queries as unbiased [34].

DeepWalk [47] is a graph embedding technique widely used in machine learning. It is developed based on the SkipGram model [41]. For each vertex, it starts a specified number of RW queries with a target length to generate embeddings. The original DeepWalk is unbiased, while the recent work [6] extends it to consider the edge weight, which becomes biased (static) random walk.

Node2Vec [16] is a popular graph embedding technique based on the second-order random walk. Different from DeepWalk, its transition probability depends on the last vertex visited. Suppose that *Q.cur* is *v*. Equation 1 describes the transition probability of selecting the edge e(v, v') where *u* is the last vertex visited, dist(v', u)is the distance between v' and *u*, and *a* and *b* are two hyperparameters controlling the random walk behaviour. Node2Vec is dynamic because the transition probability relies on the states of queries. Moreover, It can take the edge weight into the consideration by multiplying p(e) with w_e .

$$p(e(v,v')) = \begin{cases} \frac{1}{a} & \text{if } dist(v',u) = 0, \\ 1 & \text{if } dist(v',u) = 1, \\ \frac{1}{b} & \text{if } dist(v',u) = 2. \end{cases}$$
(1)

MetaPath [57] is a powerful tool to extract semantics information from heterogeneous information networks, and is widely used in machine learning tasks such as natural language processing [28, 38]. The RW queries are associated with a *meta-path schema* H, which defines the pattern of the walk paths based on the edge type, e.g., "write->publish->mention". Let H[i] be the *i*th label in H. At each step, the RW query only considers the edges $e \in E_v$ where v = Q.cur such that l_e is equal to H[|Q|]. In other words, if $l_e \neq H[|Q|]$, then p(e) = 0. Thus, the transition probability depends on the states of the RW, and MetaPath is dynamic.

2.3 Sampling Methods

Sampling from a discrete probability distribution $P = \{p_0, p_1, ..., p_{n-1}\}$ is to select an element *h* from $\{0, 1, ..., n - 1\}$ based on *P* (i.e., $P[h = i] = p_i$). In this paper, we focus on five sampling techniques, including *naive sampling*, *inverse transformation sampling*

[40], alias sampling [59], rejection sampling [50] and a special case of rejection sampling [66] because they are efficient and widely used [46, 52, 53, 60, 66]. Naive sampling only works on the uniform discrete distribution, while the other four can handle non-uniform and select the element *h* in two phases: *initialization*, which preprocesses the distribution *P*, and *generation*, which picks an element on the basis of the initialization result. Please refer to [52] for the details. In the following, we briefly introduce the sampling methods in the context of this paper, i.e., selecting an edge from E_v based on the transition probability distribution *P* where v = Q.cur.

Naive sampling (NAIVE). This method generates a uniform random integer number x in the range $[0, d_v)$ and picks $E_v[x]$, which is the xth element in E_v . It only works on the uniform discrete distribution. The time and space complexities are both O(1).

Inverse transformation sampling (ITS). The initialization phase of ITS computes the *cumulative distribution function* of P as follows: $P' = \{p'_i = \sum_{j=0}^i p_j\}$ where $0 \le i < d_v$. After that, the generation phase first generates a uniform real number x in $[0, p'_{d_{v-1}})$, then uses a binary search to find the smallest index i such that $x < p'_i$, and finally selects $E_v[i]$. The time complexity of the initialization is $O(d_v)$, and that of the generation is $O(\log d_v)$. As ITS needs to store P', the space complexity is $O(d_v)$.

Alias sampling (ALIAS). The initialization phase builds two tables: the *probability table* H, and the *alias table* A. Both of them have d_v values. H[i] and A[i] represent the *i*th value of H and A, respectively. Given $0 \le i < d_v$, A[i] is a bucket containing one or two elements from $\{0, 1, ..., d_v - 1\}$, which are denoted by A[i]. *first* and A[i]. *second*, respectively. H[i] is the probability selecting A[i]. *first*. If A[i] has only one element, then A[i]. *second* is *null* and H[i] is equal to 1. The generation phase first generates a uniform integer number x in $[0, d_v)$ and then retrieves H[x]and A[x]. Next, it generates a uniform real number y in [0, 1). If y < H[x], then picks e(v, A[x]. *first*). Otherwise, the edge selected is e(v, A[x]. *second*). The time complexity of initialization is $O(d_v)$ and that of generation is O(1). The space complexity is $O(d_v)$.

Rejection sampling (REJ). The initialization phase of REJ gets $p^* = \max_{p \in P} p$. The generation phase can be viewed as throwing darts on a rectangle dartboard until hitting the target area. Specifically, it has two steps: (1) generate a uniform integer number x in $[0, d_v)$ and a uniform real number y in $[0, p^*)$ (i.e., the dart is thrown at the position (x, y)); and (2) if $y < p_x$, then select $E_v[x]$ (i.e., hit the target area); otherwise, repeat Step (1). The time complexity of initialization is $O(d_v)$, and that of generation is $O(\mathbb{E})$ where $\mathbb{E} = \frac{d_v \times p^*}{\sum_{p \in P} p}$ (i.e., the area of the rectangle board divides the target area). Based on the computation method of \mathbb{E} , we can get that $1 \leq \mathbb{E} \leq d_v$. The space complexity is O(1).

A special case of REJ (0–REJ). A special case of REJ is that we can set a value $p^* \ge \max_{p \in P} p$ without the initialization phase, but of keeping $\mathbb{E} = \frac{d_v \times p^*}{\sum_{p \in P} p}$ is close to $\frac{d_v \times \max_{p \in P} p}{\sum_{p \in P} p}$. For example, set p^* to $\max\{1, \frac{1}{a}, \frac{1}{b}\}$ for Node2Vec [66]. The generation phase is the same as REJ. Therefore, the time complexity is $O(\mathbb{E})$ where $\mathbb{E} = \frac{d_v \times p^*}{\sum_{p \in P} p}$ and p^* is specified by users. The space complexity is O(1).

In existing works, unbiased random walks (e.g., PPR [45] and unweighted DeepWalk [47]) adopt NAIVE sampling. In contrast, biased random walks (e.g., weighted DeepWalk [8, 67], Node2Vec [16] and MetaPath [13, 19]) use ALIAS sampling because the time complexity of the generation phase is O(1). C-SAW [46] adopts ITS to utilize the parallel computation capability of GPUs to calculate the prefix sum. KnightKing [66] uses O-REJ to avoid scanning neighbors of *Q.cur* to reduce the network communication cost.

2.4 Related Work

Graph computing frameworks. There are a number of generic graph computing frameworks working on different computation environments, for example, (1) Single Machine (CPUs): GraphChi [27], Ligra [55], Graphene [32], and GraphSoft [23]; (2) GPUs: Medusa [69], CuSha [24] and Gunrock [62]; and (3) Distributed Environment: Pregel [39], GraphLab [36], PowerGraph [14], GraphX [15], Blogel [65], Gemini [71], and Grapes [10]. They usually adopt vertex- or edge-centric model, and are highly optimized for a single graph operation. In contrast, ForkGraph [37] targets at graph algorithms consisting of concurrent graph queries, for example, betweenness centrality. However, all of them focus on traditional graph query operations such as BFS and SSSP without considering RW workloads. That motivates the development of engines specially optimized for RW [46, 60, 66].

Random walk frameworks. In contrast to graph computing frameworks abstracting the computation from the view of the graph data, existing RW frameworks adopt the walker-centric model, which regards each query as the parallel task. KnightKing [66] is a distributed framework. It adopts the BSP model that moves a step for all queries at each iteration until all queries complete. To reduce data transfers in network, it utilizes O-REJ sampling to avoid scanning E_v where v = Q.cur. It exposes an API for users to set a suitable upper bound for the edge transition probability for each edge adjacent to Q.cur. Unfortunately, we find that this design introduces an implicit constraint on RW algorithms: a suitable upper bound must be determined without looping over E_v . This works well for Node2Vec by setting the upper bound as max $\{1.0/a, 1.0, 1.0/b\}$ according to Equation 1. However, it cannot handle MetaPath because the transition probability of each $e \in E_v$ can be zero because of the label filter. Another limitation is that KnightKing can suffer the tail problem since it moves a step for all queries at an iteration, whereas queries can have variant lengths.

C-SAW [46] is a framework on GPUs. It adopts the BSP model as well. To utilize the parallel computation capability in the manycore architecture, C-SAW uses ITS sampling in computation. Particularly, for all random walk types including unbiased, static and dynamic, C-SAW first conducts a prefix sum on the transition probability of edges adjacent to *Q.cur*, and then selects an edge. Consequently, it incurs high overhead for unbiased and static random walks. Moreover, C-SAW cannot support random walks with variant lengths (e.g., PPR) since such RW queries can degrade the utilization of GPUs. Additionally, Node2Vec is not supported by C-SAW, because C-SAW does not support the distance verification on GPUs.

GraphWalker [60] is an I/O efficient framework on a single machine. For a graph that cannot reside in memory, GraphWalker divides it into a set of partitions, and focuses on optimizing the scheduling of loading partitions into memory to reduce the number of I/Os. Specifically, for each partition, GraphWalker records the number of queries residing in it, and the scheduler prioritizes partitions with more queries. Given a partition G' in memory, Graph-Walker adopts the ASP model to execute queries in it. It assigns a query Q to each worker (i.e., a thread), and executes it independently until Q completes or jumps out G'. Once all queries in G'complete or leave G', GraphWalker swaps it out, and reads the partition with most queries in disk. It repeats this process till all queries complete. GraphWalker supports unbiased RW only.

This paper focuses on accelerating the in-memory execution of RW queries. ThunderRW abstracts the computation of RW algorithms from the perspective of queries as well to exploit the parallelism in RW algorithms, but takes the *step-centric* model, which regards one step of a query as the task unit and factors one step into the gather-move-update operations to empower the step interleaving technique. Moreover, ThunderRW supports all the five sampling methods in Section 2.3 so that users can adopt an appropriate sampling method given a specific workload. ThunderRW supports all the four RW-algorithms in Section 2.2, which demonstrates its programming flexibility over other RW frameworks.

RW algorithm optimization. Due to the importance of the RW-based applications, a variety of algorithm-specific optimizations have been proposed for different RW applications, e.g., PPR [17, 35, 54, 61, 63], Node2Vec [70] and second-order random walks [53]. In contrast, we aim to design a generic and efficient random walk framework on which users can easily implement different kinds of random walk applications. Thus, the algorithm-specific optimizations are beyond the scope of this paper.

Prefetching in databases. Our step-interleaving techniques are inspired by the prefetching techniques in query processing of databases. As the performance gap between main memory and CPU widens, prefetching has been an effective means to improve database performance. There have been studies applying prefetching to B-tree index [5] and hash joins [1, 4, 21, 25]. Hash joins are probably the most widely studied operator for prefetching. The group prefetching (GP) and software pipeline prefetching (SPP) [4] are the classic prefetching technique for hash joins, which rearrange a sequence of operations in a loop to several stages and execute all queries stage by stage in batch. However, GP and SPP cannot efficiently handle queries with irregular access patterns, for example a binary search performs three searches to find the target value, while the other one needs four times. To resolve the problem, AMAC [26] proposes to execute the stages of each query asynchronously by explicitly maintaining the states of each stage. However, AMAC incurs more overhead than GP and SPP, especially when there are a number of stages because it needs to maintain the states of each stage. As in the context of random walk, there is a lack of a model to abstract stages from a sequence of operations and model their dependency relationships to guide the implementation.

3 MOTIVATIONS

In this section, we study the profiling results to assess the performance bottlenecks of in-memory computation of RW algorithms. We execute RW queries with different sampling methods and examine the hardware utilization with the *top-down microarchitecture analysis method* (TMAM). In the following, we first introduce TMAM and then present the profiling results.

Table 1: Comparison of pipeline slot breakdown and memory bandwidth (the total value of read and write) between traditional graph algorithms and RW algorithms.

	01	0	0							
Method	Front End	Bad Spec	Core	Memory	Retiring	Memory Bandwidth				
BFS	11.6%	9.1%	20.8%	40.6%	18.0%	51.7 GB/s				
SSSP	9.1%	12.5%	24.9%	36.9%	16.6%	38.2 GB/s				
PPR	0.6%	0.7%	15.8%	73.1%	9.7%	1.4 GB/s				
DeepWalk	1.0%	3.9%	16.7%	69.7%	8.7%	5.6 GB/s				
Node2Vec	11.5%	22.1%	24.3%	28.1%	14.1%	17.1 GB/s				
MetaPath	6.2%	7.5%	29.7%	33.9%	22.7%	9.9 GB/s				

Top-down analysis method (TMAM) [7]. TMAM is a simplified and intuitive model for identifying the performance bottlenecks in out-of-order CPUs. It uses the *pipeline slot* to represent the hardware resources required to process the micro-operations (uOps). In a cycle, a pipeline slot is either empty (*stalled*) or filled with a uOp. The execution stall is caused by the *front-end* or the *back-end* part of the pipeline. The back-end cannot accept new operations due to the lack of required resources. It can be further split into *memory bound*, which represents the stall caused by the memory subsystem, and *core bound*, which reflects the stall incurred by the unavailable execution units. When the slot is filled with a uOp, it will be classified as *retiring* if the uOp eventually retires (Otherwise, the slot is categorized as *bad speculation*). We use Intel Vtune Profiler to measure the percentage of pipeline slots in each category.

3.1 Observations

Varying random walk workloads. We first evaluate the four RW algorithms in Section 2.2. Specifically, we set PPR as unbiased, and configure the termination probability as 0.2. For DeepWalk and Node2Vec, we set the target length as 80. The transition probability of DeepWalk is the edge weight, and that of Node2Vec is calculated based on Equation 1 where a = 2 and b = 0.5. The schema length of MetaPath is 5, and we generate it by randomly choosing five labels from the edge label set. PPR starts |V| queries from a given vertex, and the others start a query from each vertex in V. Following existing studies [6, 16, 45, 57] (as well as popular open-source packages ¹²), we use NAIVE sampling for PPR, while ALIAS sampling for the others. Moreover, we build alias tables for DeepWalk in a preprocessing phase to accelerate the execution of queries. However, this method is prohibitively expensive for high order RW due the the exponential memory consumption [53, 66]. For example, the space complexity of such an index for Node2Vec, which is second-order, is $O(\sum_{n \in V} d_n^2)$, and it can consume more than 1000 TB space for twitter. As such, we compute the transition probability and perform the initialization of ALIAS in run time. To compare the performance characteristics with RW algorithms, we evaluate BFS and SSSP, which are two conventional graph algorithms. We develop RW algorithms without any frameworks, whereas implementing BFS and SSSP with Ligra [55].

Table 1 presents the experiment results on *livejournal*, the details of which are listed in Table 5. RW queries randomly visit nodes on the graph that leads to a massive number of random memory accesses. Consequently, as high as 73.1% pipeline slots of PPR and DeepWalk are stalled due to memory access. In contrast, the memory bound of BFS and SSSP is less than 45%, which demonstrates

¹https://github.com/aditya-grover/node2vec, Last accessed on 2021/03/20

²https://github.com/GraphSAINT/GraphSAINT, Last accessed on 2021/03/20.

much better cache locality than that of PPR and DeepWalk. Due to the large proportional of memory stalls, the retiring of PPR and DeepWalk is less than 10%. Furthermore, we measure the memory bandwidth utilization of these algorithms. Our benchmark shows that the max memory bandwidth of our test bed is 60 GB/s. As shown in the table, the bandwidth utilization of BFS and SSSP are rather high (86.2% and 63.6%, respectively), while that of PPR and DeepWalk is very low (2.3% and 9.3%, respectively).

Compared with PPR and DeepWalk, Node2Vec and MetaPath exhibit different characteristics. The memory bound is lower than PPR and DeepWalk, whereas the retirement and bandwidth are much higher. To achieve more insights, we first examine the execution time breakdown on computing the transition probability (denoted by *compute* p(e)), and the initialization and generation phases of sampling an edge (denoted by *Init* and *Gen*, respectively), and then analyze the complexity of these operations at a step.

Table 2: Comparison of execution time breakdown and the time complexity per step among RW algorithms where v = Q.cur and u is the last vertex of Q.

	Time E	Breakdov	vn	Complexity per Step				
Method	Compute	Sampling Init Gen		Compute	Sampling			
	p (e)			<i>p</i> (<i>e</i>)	Init	Gen		
PPR	N/A	N/A	100%	N/A	N/A	<i>O</i> (1)		
DeepWalk	N/A	N/A	100%	N/A	N/A	O(1)		
Node2Vec	89.9%	9.9%	0.2%	$O(d_v \times \log d_u)$	$O(d_v)$	O(1)		
MetaPath	29.0%	69.9%	1.1%	$O(d_v)$	$O(d_v)$	O(1)		

Table 2 lists the results. PPR and DeepWalk are static, and they only need to sample an edge and move Q along it in run time. In contrast, Node2Vec and MetaPath are dynamic, and they first compute the transition probability for each $e \in E_v$ where v = Q.cur, and then sample an edge. Consequently, the cost on *Gen* is neglected as shown in Table 2. Moreover, the memory bound is much lower than static RWs in Table 1 since the computation scans E_v in a continuous manner. Given $e \in E_v$ and u is the last vertex of Q, the complexity of computing p(e) in Node2Vec is $O(\log d_u)$ because the distance check in Equation 1 is implemented by a binary search. However, MetaPath computes p(e) with a simple label filter. As a result, computing p(e) accounts for around 90% of the execution time in Node2Vec, whereas *Init* dominates the cost in MetaPath.

Observation 1. The in-memory computation of common RW algorithms suffers severe performance issues due to memory stalls caused by cache misses and under-utilizes the memory bandwidth. For high order RW algorithms, computing p(e) and initializing the auxiliary data structure for sampling dominate the in-memory computation cost, and their complexities are determined by the RW algorithm and the selected sampling method, respectively.

Varying sampling methods and RW types. We further examine the performance of sampling methods. We continue to develop a micro benchmark that executes 10^7 RW queries each of which starts from a vertex randomly selected from the graph. The target length is 80. We evaluate three types of RW queries as discussed in Section 2.2: **unbiased**, **static** and **dynamic**. For unbiased RW, we first perform the initialization phase of sampling methods for the neighbor set of each vertex in a *preprocessing* step. We then use the generation phase of a sampling method to select a neighbor of *Q.cur* in execution. For static RW, we evaluate queries with the same process as that of unbiased. The only difference is that the edge weight is used to set the transition probability for static RW whereas the transition probability in unbiased RW is the default uniform. For dynamic RW, we set the edge weight as the transition probability, while performing the initialization phase for the neighbor set of *Q.cur* in execution because the transition probability of dynamic RW varies during the computation.

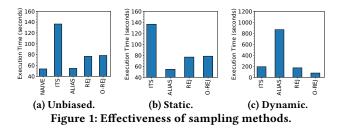


Figure 1 presents the experiment results of the sequential execution with variant sampling methods on different RW types. We have the following findings. First, the NAIVE sampling method performs the best on unbiased RW as it has no initialization phase. Second, among static methods, the ALIAS sampling method outperforms others because its generation phase has lower time complexity. However, ALIAS runs much slower than other methods on dynamic RW since its initialization cost is high in practice. Third, 0-REJ performs well on dynamic RW since it does not have the initialization phase. Fourth, we can observe that the cost of evaluating dynamic RW is significantly expensive than that of unbiased and static RW because of the initialization phase (if exists) at each step.

Observation 2. Sampling methods have an important impact on the performance and no sampling method can dominate on all cases. Generally, dynamic RW is expensive than unbiased and static RW.

3.2 System Implications

Based on the profiling results, we can categorize the cost of evaluating RW queries into two classes, that of computing p(e) and that of sampling an edge. As the former is determined by the RW algorithms (i.e., algorithm-specific), our framework targets at accelerating the latter operation. Moreover, we have the following implications for the design and implementation of ThunderRW. First, we need to develop mechanisms to reduce the cache stalls. Our profiling results show that in-memory computation of common RW algorithms suffer severe performance issues due to the irregular memory accesses. None of previous random walk frameworks [46, 60, 66] address the problem. On the other hand, there are massive queries in random walk workloads, but the memory bandwidth is under-utilized. Inspired by previous work on accelerating multiple index lookups in database systems with prefetching [4, 26], there are opportunities for prefetching and interleaving executions among different queries.

Second, there is a need to support multiple sampling methods. However, existing frameworks support one sampling method only and generally regard all RW as dynamic (e.g., C-SAW), while (1) the sampling method has an important impact on the performance and none of them can dominate on all cases; and (2) the cost of evaluating dynamic RW is generally much more expensive than that of unbiased and static RW.

4 THUNDERRW ABSTRACTION

In this section, we present the abstraction of the computation in ThunderRW.

4.1 Step-centric Model

To abstract the computation of RW algorithms, we propose the *stepcentric* model in this paper. We observe that RW algorithms are built upon a number of RW queries rather than a single query. In spite of limited intra-query parallelism, there is abundant inter-query parallelism in RW-algorithms as each RW query can be executed independently. Therefore, our step-centric model abstracts the computation of RW algorithms from the perspective of queries to exploit the inter-query parallelism.

Specifically, we model the computation from the local view of moving one step of a query Q. Then, we abstract a step of Q into the Gather-Move-Update (GMU) operations to characterize the common structure of RW algorithms. With the step-centric model, users develop RW algorithms by "thinking like a walker". They focus on defining functions setting the transition probability of $e \in E_v$ and updating states of Q at each step, while the framework facilitates applying user-defined step-oriented functions to RW queries.

4.2 Step-centric Programming

Framework. Algorithm 2 gives an overview of ThunderRW. Lines 1-6 execute each query one-by-one. Lines 3-5 factor one step into three functions based on the step-centric model. Gather collects the transition probabilities of edges adjacent to Q.cur. It loops over $E_{Q.cur}$, applies Weight, a user-defined function, to each edge e and add the transition probability of e to C (Lines 10-11). Then, Line 12 executes the initialization phase of a given sampling method to update C. Move picks an edge based on C and moves Q along the selected edge (Lines 14-16). As random memory accesses in the *system space* (i.e., the framework excluding user-defined functions) are mainly in Move, we apply step-interleaving techniques to optimize its performance (see Section 5). Finally, Line 5 invokes Update, a user-defined function, to update states of Q based on the movement. The return value of Update decides whether Q should be terminated.

A	gorithm 2: ThunderRW Framework
I	nput: a graph G and a set \mathbb{Q} of random walk queries;
C	Dutput: the walk sequences of each query in \mathbb{Q} ;
1 f	\mathbf{O} oreach $Q \in \mathbb{Q}$ do
2	do
3	$C \leftarrow \text{Gather}(G, Q, Weight);$
4	$e \leftarrow Move(G, Q, C);$
5	$stop \leftarrow Update(Q, e);$
6	while stop is false;
7 r	eturn Q;
8 F	Function Gather (G, Q, Weight)
9	$C \leftarrow \{\};$
10	foreach $e \in E_{O,cur}$ do
11	Add $Weight(Q, e)$ to C;
12	$C \leftarrow$ execute initialization phase of a given sampling method on C ;
13	return C;
14 F	Function Move (G, Q, C)
15	Select an edge $e(Q.cur, v) \in E_{Q.cur}$ based on C and add v to Q;
16	return $e(Q.cur, v);$

Algorit	hm 3: Pro	processing for	Static Rand	lom Walk
---------	------------------	----------------	-------------	----------

Input: a graph G;

Output: the transition probabilities C_v on E_v for each vertex v;

1 foreach $v \in V(G)$ do 2 $| C_v \leftarrow \{\};$

foreach $e \in E_v$ do

4 Add Weight(null, e) to C_v ;

5 $C_v \leftarrow$ execute initialization phase of a given sampling method on C_v ;

6 Store C_v for the usage in query execution.

The framework described in Algorithm 2 can support unbiased, static and dynamic RW with different sampling methods. Furthermore, we optimize the execution flow of ThunderRW based on the RW type and the selected sampling method. The transition probability of static RW is fixed during the execution. In that case, ThunderRW omits the Gather operation but introducing a preprocessing step to reduce the runtime cost, which obtains transition probabilities in the system initialization. Algorithm 3 presents the preprocessing for static RW. Given a vertex *v*, Lines 3-4 loop over each edge *e* in E_v and apply the Weight function to *e* to obtain the transition probability. As the probability does not rely on a query, we set *Q* as *null*. After that, Lines 5-6 perform the initialization phase of a given sampling method on C_v and store C_v for the usage in the query execution. As such, we can load $C_{Q.cur}$ directly without Gather for static RW in Algorithm 2.

Moreover, the NAIVE and O-REJ sampling methods have no initialization phase as discussed in Section 2.3. Hence, we do not need to collect the transition probability for initialization. As such, ThunderRW skips both the preprocessing step and the Gather operation in the execution if NAIVE or O-REJ is used.

Application Programming Interfaces (APIs). ThunderRW provides two kinds of APIs, which include hyperparameters and user-defined functions. Users develop their RW algorithms in two steps. Firstly, set the RW type and the sampling method via hyperparameters walker_type and sampling_method, respectively. Secondly, define the Weight and Update functions. The Weight function specifies the relative chance of an edge being selected. The Update function modifies states of *Q* given the selected edge. If its return value is *true*, then the framework terminates *Q*. Otherwise, *Q* continues walking on *G*. When using 0-REJ, users need to implement the MaxWeight function to set the maximum value of the transition probability. We present an example in the following.

```
WalkerType walker_type = WalkerType::Dynamic;
SamplingMethod sampling_method = SamplingMethod::O-REJ;
double Weight(Walker Q, Edge e) {
    if (Q.length == 0) return max(1.0 / a, 1.0, 1.0 / b);
    else if (e.dst == Q.prev) return 1.0 / a;
    else if (IsNeighbor(e.dst, Q.prev)) return 1.0;
    else return 1.0 / b;
}
bool Update(Walker Q, Edge e) {
    return Q.length == target_length;
}
double MaxWeight() {
    return max(1.0 / a, 1.0, 1.0 / b);
}
```

Listing 1: Node2Vec sample code.

Example 4.1. List 1 shows the sample code of Node2Vec, which is dynamic. As the maximum value can be easily determined by

the parameters a and b, we use O-REJ to avoid scanning each edge adjacent to Q.cur at each step. Thus, we set sampling_method to O-REJ and implement MaxWeight. The Weight function is configured based on Equation 1. Once the length of Q meets the target length, we terminate it.

ThunderRW applies user-defined functions to RW queries, and evaluates the queries based on RW type and selected sampling method in parallel. Thus, users can easily implement customized RW algorithms with ThunderRW, which significantly reduces the engineering effort. For example, users write only around ten lines of code to implement Node2Vec as shown in Example 4.1.

Parallelization. RW algorithms contain massive random walk queries each of which can be completed independently and rapidly. Therefore, ThunderRW adopts the static scheduling method to keep load balancing among workers. Specifically, we regard each thread as a worker and evenly assign \mathbb{Q} to the workers. A worker independently executes the assigned queries with Algorithm 2. Our experiment results show that the simple scheduling method achieves good performance.

4.3 Analysis

In this subsection, we analyze the space and time cost of Algorithm 2 on different RW types with variant sampling methods. As the cost of Weight and Update is determined by users' implementation, we assume their cost is a constant value for the ease of analysis.

Space. The space for storing the graph is O(|E| + |V|), and that for maintaining the output is $O(\sum_{Q \in \mathbb{Q}} |Q|)$. Gather in Algorithm 2 requires $O(d_{max})$ space to store C where d_{max} is the max degree value of G. Suppose that ThunderRW has n threads. Then, the memory cost is $O(n \times d_{max})$. When there is a preprocessing step, the memory cost of ITS and ALIAS is O(|E|), while that of REJ is O(|V|) based on the analysis in Section 2.3.

Time. Given a sampling method, α and β denote the cost of its initialization phase and generation phase, respectively. Let d_{avg} represent the average degree of *G*. Thus, the cost of Gather in Algorithm 2 is $d_{avg} + \alpha$, and that of Move is β . For static RW, the preprocessing cost is $\sum_{v \in V} (d_v + \alpha)$, while the cost of processing one step is β as it does not conduct Gather during execution. From Section 2.3 we can get the value of α and β for the sampling methods. Support that $T = \sum_{Q \in \mathbb{Q}} |Q|$, which is the total number of steps of all queries. Table 3 summarizes the time complexity on different RW types with variant sampling methods.

As shown in the table, NAIVE supports unbiased RW only. For ITS, ALIAS and REJ, the cost on unbiased and static RW consists of the preprocessing cost and the execution cost. Because RW algorithms can have massive RW queries with a long length, the execution cost is generally much more expensive than the preprocessing cost. As 0-REJ has no initialization phase, it neither performs the preprocessing for unbiased and static RW nor executes Gather for dynamic RW. Thus, the time complexity is the same for the three RW types.

Recommendation. From the analysis, we have the following guidelines for setting sampling methods for users: (1) NAIVE is the best sampling method for unbiased RW; (2) ALIAS is a good choice for static RW since the execution time is generally longer than the preprocessing time; and (3) if we can set a reasonable max value for

Table 3: The time complexity of ThunderRW on different
random walk types with variant sampling methods

	71	1	0
Method	Unbiased	Static	Dynamic
NAIVE	O(T)	N/A	N/A
ITS	$O(E + T \times \log d_{avg})$	Same as unbiased	$O(T \times (d_{avg} + \log d_{avg}))$
ALIAS	O(E +T)	Same as unbiased	$O(T \times (d_{avg} + 1))$
REJ	$O(E + T \times \mathbb{E})$	Same as unbiased	$O(T \times (d_{avg} + \mathbb{E}))$
O-REJ	$O(T \times \mathbb{E})$	Same as unbiased	Same as unbiased

the transition probability, then use O-REJ for dynamic RW. Users can easily tell the RW type based on the properties of transition probability. To further ease the programming efforts, we set the default sampling method of unbiased, static and dynamic RW to NAIVE, ALIAS and ITS, respectively. We use ITS instead of ALIAS for dynamic RW because the initialization cost of ALIAS at each step is much more than that of ITS in practice. If users can set a good max value for the transition probability, then they can select O-REJ for dynamic RW.

5 STEP-INTERLEAVING

In this section, we present the step interleaving technique, which reduces the pipeline stall caused by random memory accesses.

5.1 General Idea

Based on the step-centric model, ThunderRW processes a step of a query Q with the GMU operations. According to the profiling results in Section 3, there can be two main sources for random memory accesses under the model. First, the Move operation picks an edge randomly and moves Q along the selected edge. Second, the operations in user-defined functions can introduce cache misses, for example, the distance check operation in Node2Vec. As operations in the user space (i.e., user-defined functions) are determined by RW algorithms, and can be very flexible, we target at memory issues incurred by the system (i.e., the Move operation). Motivated by the profiling result, we propose to use the software prefectching technique [29] to accelerate in-memory computation of ThunderRW. However, a step of a query Q does not have enough computation workload to hide memory access latency because steps of Q have dependency relationship. Therefore, we propose to hide memory access latency via executing steps of different queries alternately.

Specifically, given a sequence of operations in Move, we decompose them into multiple stages such that the computation of a stage consumes the data generated by previous stages and it retrieves the data for the subsequent stages if necessary. We execute a group of queries simultaneously. Once a stage of a query Q completes, we switch to stages of other queries in the group. We resume the execution of Q when stages of other queries complete. In such a way we hide the memory access latency in a single query and keep CPUs busy. We call this approach *step interleaving*.

Example 5.1. Figure 2 presents an example where a step is divided into four stages. If executing a query step-by-step sequentially, then CPUs are frequently stalled due to memory access. Even with prefetching, the computation of a stage cannot hide the memory access latency. In contrast, the step interleaving hides the memory access latency by executing steps of different queries alternately.

Let's perform a simple back-of-envelop calculation on the performance gain of interleaving execution. Given a group containing k queries, we assume that Move of each query executes the

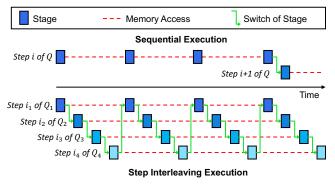


Figure 2: Sequential versus step interleaving.

same number of stages and the cost W_C of each stage is the same for the ease of analysis. Suppose that there are *m* stages with memory access and \overline{m} without. W_L denotes the latency of memory access. Then, the cost of moving a step for the queries in sequential is equal to $W_0 = k((m + \overline{m})W_C + mW_L)$. Let W_S denote the cost of switching. The cost of Move with step interleaving is $W_1 = k((m + \overline{m})(W_C + W_S) + m(\max(W_L - kW_S - (k - 1)W_C, 0))$ where the last term calculates whether step interleaving hides memory access latency. Therefore, the gain of step interleaving for a step of *k* queries can be estimated by Equation 2 where $W_{hide} = \max(W_L - kW_S - (k - 1)W_C, 0)$.

$$W_{gain} = (W_0 - W_1)/k$$

= $mW_L - (m + \overline{m})W_S - mW_{hide}.$ (2)

From Equation 2, we can see that step interleaving requires an efficient switch mechanism to reduce the overhead W_S of performing switching, and enough workload to overlap the memory access latency W_{hide} .

5.2 Stage Dependency Graph

We design the *stage dependency graph* (SDG) to model stages of a sequence of operations in a step. Each node in SDG is a stage containing a set of operations and edges represent the dependency relationship among them. Given the sequence of operations, we build SDG in two steps, abstracting stages (nodes) and extracting dependency relationships (edges).

Defining stages: As we hide memory access latency by switching the execution of queries, the constraint on stages is that each stage contains at most one memory access operation and the operations consuming the data are in subsequent stages. Note that we view the operation containing jump operation as a single stage for the ease of the implementation of switching. We present an example in the following.

Example 5.2. The right column of Table 4 illustrates the sequence of operations in the Move function with the ALIAS and REJ sampling methods, respectively, to perform the neighbor selection. The left column lists stages. For example, S_0 of ALIAS loads d_v consumed in O_1 of S_1 . O_5 in REJ has the jump operation. Therefore, we regard it as a separate stage.

Defining edges: Next, we add edges among nodes in SDG based on their dependency relationships. Given stages S and S', if there is a dependency relationship between S and S', we add an edge

Stage	ALIAS
S_0	O_0 : Load d_v .
S_1	O_1 : Generate an int random num x in $[0, d_v)$. O_2 : Generate a real random num y in $[0, 1)$. O_3 : Load $C[x] = (H[x], A[x])$.
S_2	$O_4: \text{ If } y < H[x], v' = A[x]. \text{ first; Else } v' = A[x]. \text{ second.}$ $O_5: \text{ Add } v' \text{ to } Q \text{ and return } e(v, v').$
Stage	REJ
S_0	O_0 : Load d_v .
S_1	O_1 : Load the maximum value p_v^* .
	O_2 : Generate an int random num x in $[0, d_v)$.
S_2	O_3 : Generate a real random num y in $[0, p_v^*)$.
	O_4 : Load $C[x] = p$.
S_3	O_5 : If $y > C[x]$, jump to O_2 ; Else jump to O_6 .
	O L (π, π') E $[\pi]$
S_4	$O_6: \text{Load } e(v, v') = E_v[x].$ $O_7: \text{Add } v' \text{ to } Q \text{ and return } e(v, v').$

 $(S_i) \text{ Stage} \longrightarrow \overset{\text{Memory}}{\text{Dependency}} \xrightarrow{\text{Computation}} \overset{\text{Control}}{\text{Dependency}} \xrightarrow{\text{Computation}} \overset{\text{Control}}{\text{Dependency}} \xrightarrow{\text{Computation}} \overset{\text{Control}}{\text{Dependency}} \xrightarrow{\text{Computation}} \overset{\text{Control}}{\text{Dependency}} \xrightarrow{\text{Computation}} \overset{\text{Control}}{\text{Dependency}} \xrightarrow{\text{Computation}} \xrightarrow{\text{Computation}} \xrightarrow{\text{Computation}} \xrightarrow{\text{Computation}} \xrightarrow{\text{Control}} \xrightarrow{\text{Dependency}} \xrightarrow{\text{Computation}} \xrightarrow{\text{$

Figure 3: Stage dependency graph.

from *S* to *S'*. The edges are categorized into three types, *memory dependency*, *computation dependency* and *control dependency*. We call the first two relationship as *data dependency*. More specifically, if *S'* consumes the data loaded from memory by *S*, then the edge type is memory dependency. Otherwise, *S'* depends on the data computed by *S* and the edge type is computation dependency. The data leading to the dependency is attached to each edge as properties. Furthermore, if *S* contains the operation jumping to *S'*, we add the control dependency from *S* to *S'*. SDG allows that there are multiple edges (i.e., dependency, SDG is a directed acyclic graph (DAG), while the control dependency can generate cycles in SDG.

Example 5.3. Continuing with Example 5.2, Figure 3 shows SDGs. In SDG of ALIAS, S_2 relies on x, y, which are random numbers generated by S_1 , while (H[x], A[x]) is the data retrieved from memory. As such, S_1 and S_2 have both memory and computation dependency relationships. SDG of ALIAS is a DAG because there is no control dependency. In contrast, there is a cycle containing S_2 and S_3 in SDG of REJ because of the control dependency.

In summary, SDG is a methodology to abstract stages from a sequence of operations in Move and model the dependency relationship among them. Note that the stage design of MOVE does not require user input but it is implemented in the system space.

5.3 State Switch Mechanism

In this subsection, we introduce the implementation of step interleaving under SDG. Based on Equation 2, we need an efficient switch mechanism. For example, using multi-threading is forbidden because the overhead of context switch among threads is in microseconds, whereas the main memory latency is in nanoseconds. As each thread tends to take many RW queries, we switch the execution among stages in a single thread.

Table 4: Stages of Move with ALIAS and REJ (v = Q.cur).

We categorize stages of a SDG into two classes based on whether they belong to cycles in SDG. For stages not in cycles (called *noncycle stages*), a query visits them exactly once to complete Move. Given a group of queries \mathbb{Q}' , we execute them in a coupled manner. Particularly, once a query $Q_i \in \mathbb{Q}'$ completes a stage *S*, we switch to the next query $Q_{i+1} \in \mathbb{Q}'$ to process *S*. After all queries complete *S*, we move to the next stage. In contrast, stages in cycles (called *cycle stages*) can be visited variant times for different queries. To deal with the irregularity, we process them in a decoupled manner. Specifically, each query *Q* records the stage *S* to be executed. When switching to *Q*, we execute *S*, set the next stage of *Q* based on SDG, and switch to the next query after completing *S*. As a result, each query executes asynchronous.

For data communication between different stages in a query, we create two kinds of ring buffers based on SDG, in which the computation dependency edge indicates the information requiring to be stored. In particular, the *task ring* is used for data communication across all stages of a query, while the search ring serves to process cycle stages. As we need to explicitly record states of cycle stages and control the switch of them, processing cycle stages not only causes implementation complexities, but also incurs more overhead. Note that the SDGs of NAIVE and ALIAS have no cycle stages because there are no for loops in their generation phases, whereas that of ITS, REJ and O-REJ have. The implementation details are introduced in the complete version paper [56].

5.4 Ring Size Tuning

The task ring size k and the search ring size k' determine the group size of queries executed simultaneously in a thread, and therefore control memory level parallelism of executing non-cycle stages and cycle stages, respectively. According to Equation 2, we can improve the performance by increasing k to reduce W_{hide} . However, k is limited by hardware. Particularly, modern CPUs can issue a limited number of outstanding memory requests, and the L1 data cache size is only tens of kilobytes. Setting k to a large value can evict data before the usage. In ThunderRW, we tune ring sizes by preexecuting a number of queries. We start a RW query from each vertex with the target length as 10 and set the RW type as static. We first select the NAIVE and ALIAS sampling methods, respectively and vary k from 1, 2, ..., 512, 1024 to pick an optimal value k^* . Next we fix k to k^* and vary k' from 1, 2, ..., k^* to select optimal values for ITS, REJ and 0-REJ, respectively.

6 EXPERIMENTS

We conduct experiments to evaluate the performance of ThunderRW in this section.

6.1 Experimental Setup

We conduct experiments on a Linux server equipped with an Intel Xeon W-2155 CPU and 220GB RAM. The CPU has ten physical cores with hyper-threading disabled for consistent measurement. The sizes of L1, L2 and L3 (last level cache, LLC) caches are 32KB, 1MB and 13.75MB, respectively.

Datasets. Table 5 lists the statistics of the twelve real-world graphs in our experiments. *ab* and *ac* are downloaded from [43], *wk* is obtained from [42], *eu*, *uk* and *tw* are obtained from [51],

Table 5: Properties of real-world datasets.

1												
Dataset	Name	V	E	d_{avg}	d_{max}	Memory						
amazon	am	0.55M	1.85M	3.38	549	0.01GB						
youtube	yt	1.14M	2.99M	5.24	28754	0.03GB						
us patents	ир	3.78M	16.52M	8.74	793	0.17GB						
eu-2005	eu	0.86M	19.24M	44.74	68963	0.15GB						
amazon-clothing	ас	15.16M	63.33M	4.18	12845	0.35GB						
amazon-book	ab	18.29M	102.12M	5.58	58147	0.52GB						
livejournal	lj	4.85M	68.99M	28.45	20333	0.54GB						
com-orkut	ot	3.07M	117.19M	76.34	33313	0.89GB						
wikidata	wk	40.96M	265.20M	6.47	8085513	1.29GB						
uk-2002	uk	18.52M	298.11M	32.19	194955	2.30GB						
twitter	tw	41.66M	1.21B	58.08	2997487	9.27GB						
friendster	fs	65.61M	1.81B	55.17	5214	13.71GB						

and the other graphs are downloaded from [30]. The datasets are from different categories such as web, social and citation, and have different densities. The number of vertices is ranged from hundreds of thousands to tens of millions, and the number of edges scales from millions to billions. Except *am*, all the graphs outsize LLC.

Workloads. We study PPR, DeepWalk, Node2Vec and MetaPath to evaluate the performance and generality of competing methods. The settings of the four algorithms are the same as that in Section 3. *ab* and *ac* are weighted graphs where weights denote review ratings for products. *wk* has 1327 distinct labels, which represents the relationship between entities in a knowledge base. The other graphs are unweighted and unlabeled. Given a graph having no labels or weights, we set the weight and label of edges with the same setting as previous work [66]: (1) We choose a real number from [1, 5) uniformly at random, and assign it to an edge as its weight; and (2) We set the edge label by randomly choosing a label from a set containing five distinct labels.

Comparison. In our experiments, we compare the performance of ThunderRW (called *TRW* for short) with the following methods.

- *BL*: Baseline approaches that first load a graph entirely into memory and then execute random walks, the detail of which is presented in Section 3.
- *HG*: Our homegrown implementation optimizing *BL* from two aspects: (1) select a suitable sampling method for each algorithm according to the recommendation in Section 4.3; and (2) regard each query as a parallel task with OpenMP.
- *GW*: GraphWalker [60], the state-of-the-art RW framework in a single machine. For the fair of comparison, we configure GraphWalker to execute in-memory, without any disk I/O.
- *KK*: KnightKing [66], the state-of-the-art distributed RW framework. It supports to execute in a single machine.

We implement all our methods including *BL*, *HG* and *TRW* in C++. GW^3 and KK^4 are programmed in C++ as well. All the source code is compiled by g++ 8.3.1 with -O3 enabled. *BL* executes in serial, while the other methods are running on all the cores of the single socket, with one thread per core.

We consider C-SAW [46], the state-of-the-art RW framework on GPUs, as well. However, its open source package⁵ supports 4000 queries at most, which cannot handle the workload containing massive queries in the experiment. Previous experiment results [60, 66] show that *KK* and *GW* significantly outperform generic graph computing frameworks such as Gemini [71] on RW algorithms.

³https://github.com/ustcadsl/GraphWalker, Last accessed on 2020/12/07.

⁴https://github.com/KnightKingWalk/KnightKing, Last accessed on 2020/12/20.

⁵https://github.com/concept-inversion/C-SAW, Last accessed on 2020/12/07.

			PPR			DeepWalk				Node2vec				MetaPath		
Dataset	BL	HG	GW	KK	TRW	BL	HG	KK	TRW	BL	HG	KK	TRW	BL	HG	TRW
am	0.06	0.008	0.42	0.012	0.007	2.16	0.21	0.44	0.07	9.97	0.26	2.08	0.14	0.22	0.018	0.012
yt	0.33	0.04	1.68	0.05	0.015	9.78	0.98	1.93	0.26	853.13	1.30	5.94	1.03	6.18	0.23	0.24
ир	1.24	0.13	7.19	0.19	0.07	45.44	4.33	8.41	0.95	369.00	6.20	16.92	4.01	4.88	0.40	0.24
еи	0.16	0.02	0.99	0.03	0.011	8.16	0.82	1.56	0.20	2731.07	1.47	4.43	1.14	90.55	3.18	3.55
ас	4.84	0.51	19.31	0.65	0.19	173.66	17.86	31.88	3.31	6951.12	24.54	87.86	6.26	45.01	2.01	1.69
ab	8.86	0.94	26.74	1.09	0.26	212.80	22.24	40.07	4.01	26231.45	32.04	100.78	7.87	128.35	5.06	4.47
lj	1.69	0.19	7.90	0.23	0.06	55.63	5.44	10.67	1.19	2951.33	9.09	24.95	6.20	18.08	0.94	0.75
ot	1.49	0.16	5.25	0.19	0.04	38.54	3.70	7.97	0.80	5891.28	7.28	15.16	4.82	40.77	1.72	1.57
wk	21.86	2.21	47.05	3.07	0.59	502.27	49.67	95.17	9.26	OOT	68.43	216.24	27.68	5.98	0.54	0.55
uk	6.47	0.69	27.72	0.90	0.24	203.86	20.42	21.40	4.56	12630.01	34.36	94.69	28.68	322.66	12.84	12.56
tw	26.42	2.73	77.12	3.61	1.16	575.43	61.18	115.92	11.13	OOT	130.72	232.41	91.00	OOT	12300.32	9780.20
fs	79.14	8.20	223.81	10.72	4.10	1043.93	108.23	208.45	17.67	OOT	178.15	364.51	120.16	683.05	28.69	25.01

Table 6: Overall performance comparison (seconds).

Therefore, our experiment does not involve C-SAW as well as any generic graph computing frameworks.

As for RW algorithms, *GW* only supports unbiased RW. Thus, we execute PPR without considering edge weights, and evaluate *GW* on PPR only. Despite that *KK* studies MetaPath in the original paper [66], its open source package cannot handle labeled graphs. As such, it cannot execute MetaPath. In contrast, *TRW* supports all the four algorithms, which demonstrates its flexibility.

As for sampling methods, *BL* uses NAIVE for PPR, while adopts ALIAS for the other three algorithms. As discussed in Section 3, building alias tables for dynamic RW in an indexing phase can consume a huge amount of memory. Therefore, in the experiments, *BL* dynamically computes the alias table (i.e., perform the initialization of ALIAS) at each step of a query, which is the same as the computation flow of *TRW* for dynamic RW. Different from *BL*, *HG* adopts O-REJ for Node2Vec, and ITS for MetaPath. This is because (1) the max value of transition probability of Node2Vec can be easily set as max(1, 1/*a*, 1/*b*), and O-REJ can avoid scanning the neighbors of *Q.cur* at each step; and (2) the probability distribution of MetaPath is skewed due to filtering based on labels, which increases the generation cost of rejection sampling, and the initialization phase of ITS is much faster than that of ALIAS in practice. *TRW* adopts the same sampling method as *HG* for each algorithm.

Ring Size Setting. We tune the ring size with the method in Section 5.4. Despite that the graphs have variant structures, the optimal setting for them is close. First, the optimal value for the graphs except *am* is k = 64 and k' = 32 because the optimal ring size is closely related to the instructions available for computation, the switch overhead, the memory access latency, and the maximum number of outstanding memory requests, which are determined by the program and hardwares. Second, the optimal value for *am* is k = 32 and k' = 32 as *am* fits in LLC and the memory access latency is smaller than that of the other graphs. Additionally, the tuning process is very efficient, which takes less than one minute for most of the graphs. Even for *fs* with more than 1.8 billion edges, the tuning is completed with around four minutes.

Metrics. The *total time* is the elapsed time on evaluating RW algorithms without counting the time on loading data from the disk. For static random walk, the total time consists of the *preprocessing time*, which is the time spent on the preprocessing, and the *execution time*, which is the time spent on executing queries. To complete experiments in a reasonable time, we set the time limit for each algorithm as eight hours. If an algorithm cannot be completed

within the limit, we terminate it and record the execution time as *OOT* (i.e., out-of-time). We measure the *throughput* (steps per second) by dividing the number of steps of all queries by the execution time. To provide more insights, we adopt *Intel Vtune Profiler* to examine the pipeline slot utilization and use *Linux Perf* to examine the *instructions per step* and *cycles per step*, which are the number of instructions and the number of cycles on one step, respectively.

Supplement experiments. More experiment results including the impact of ring sizes, memory bandwidth utilization, the effectiveness of prefetching data to different cache levels, the impact of the step interleaving on existing systems and the comparison with AMAC [26] are presented in the full version paper [56].

6.2 Overall Comparison

Table 6 gives an overall comparison of competing methods on the four RW algorithms. Although GW is parallel, it runs slower than BL, the sequential baseline algorithm. KK runs faster than GW and BL, but slower than HG because (1) the framework incurs extra overhead compared with HG; and (2) HG adopts an appropriate sampling method for each algorithm. TRW runs 54.6-131.7X and 1.7-14.6X faster than GW and KK, respectively.

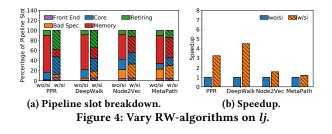
Benefiting from parallelization, HG achieves 7.5-10.5X speedup over BL on PPR and DeepWalk. Moreover, HG runs 38.3-1857.9X and 11.1-28.5X faster than BL on Node2Vec and MetaPath, respectively, because HG adopts 0-REJ sampling for Node2Vec, which avoids scanning the neighbors of Q.cur at each step, and uses ITS sampling for MetaPath, the initialization phase of which is more efficient than that of ALIAS in practice. TRW runs 8.6-3333.1X faster than BL. Even compared with HG, TRW achives up to 6.1X speedup benefiting from our step-centric model and step interleaving technique. As MetaPath is dynamic and both TRW and HG use ITS sampling, the gather operation at each step dominates the cost. Still, MetaPath on ThunderRW outperforms that on HG for nine out of twelve graphs, and is slightly slower on the other three graphs. tw is dense but highly skewed (as shown in Table 5) and the vertices with high degrees are frequently visited. Consequently, the execution time on MetaPath against tw is much longer than that on other graphs.

In summary, ThunderRW significantly outperforms state-of-theart frameworks and homegrown solutions (e.g., *BL* takes more than eight hours for Node2Vec on *tw*, while *TRW* completes the algorithm in two minutes). Furthermore, ThunderRW saves a lot of engineering effort on the implementation and parallelization of RW algorithms compared with *BL* and *HG*.

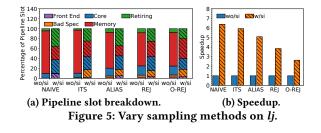
6.3 Evaluation of Step Interleaving

We evaluate the effectiveness of step interleaving in this subsection. For brevity, we use *lj* as the representative graph by default.

Varying RW algorithms. We first evaluate the effectiveness of step interleaving on different RW algorithms. Figure 4 presents the pipeline slot breakdown and speedup among the RW algorithms. wo/si and w/si denote ThunderRW without and with the step interleaving technique, respectively. Enabling step interleaving drastically reduces memory bound on PPR and DeepWalk, and improves the instruction retirement. Correspondingly, w/si achieves significant speedup over wo/si in Figure 4b. The speedup on PPR is lower than that on DeepWalk because PPR issues all queries from a given vertex and the expected length of a query is 5, which by default exhibits better memory locality than DeepWalk. The memory bound on Node2Vec is reduced from around 60% to 40% because the Weight function checks whether two vertices are neighbors with a binary search, which causes a number of random memory access. The speedup on MetaPath is small because MetaPath is dynamic and the gather operation dominates the cost at each step.



Varying sampling methods. We next examine the performance of step interleaving on variant sampling methods. As the gather operation dominates the cost on dynamic random walk, we focus on unbiased and static random walk. Particularly, we use Deep-Walk as the representative RW algorithm and evaluate it with the five sampling methods in Section 2.3, respectively. When adopting NAIVE, we regard DeepWalk as unbiased random walk (i.e., without considering edge weight). Figure 5 presents the pipeline slot breakdown and speedup on *lj* with variant sampling methods. We can see that the step interleaving technique significantly reduces memory bound on all the five sampling methods and achieves remarkable speedup. The results demonstrate both the generality and effectiveness of the step interleaving technique.



Varying datasets. To explore the impact of graph structures on the performance, we evaluate the speedup of enabling step interleaving for DeepWalk on different datasets. Figure 6 presents the experiment results. The speedup on *am* and *yt* is smaller than that on other graphs because *am* can fit in LLC, and *yt* is only two times larger than LLC. The speedup on *eu* and *uk* is lower than the other graphs that are much larger than LLC since *eu* and *uk* have dense communities (e.g., *uk* has a clique containing around 1000 vertices [3]), and RW queries exhibit good memory locality. In contrast, the speedup on *ac* and *ab* is generally higher than the other graphs because they are bipartite graphs and very sparse, and RW queries have poor memory locality. In summary, the optimization tends to achieve higher speedup on large and sparse graphs than small graphs and graphs with dense community structures because RW queries have poorer memory locality on the former one. Nevertheless, the optimization brings up to 3X speedup even on graphs entirely fitting in LLC (i.e., *am*) since L1 cache is only tens of kilobytes, but around ten times faster than LLC, and the step interleaving directly fetches the data to L1 cache.

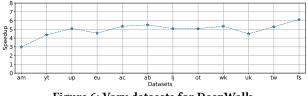
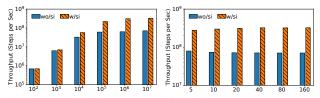


Figure 6: Vary datasets for DeepWalk.

6.4 Scalability Evaluation

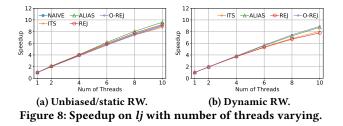
In this section, we evaluate the scalability of ThunderRW. By default, we execute 10⁷ RW queries on *lj* with the target length as 80. Each query starts from a vertex selected from the graph randomly. We first evaluate the throughput in terms of steps per second with the number of queries and the length of queries varying, respectively. In that case, we set the RW as static and use the ALIAS sampling method as the representative. Next, we evaluate the speedup with the number of threads varying. When setting the RW as unbiased, we use the NAIVE sampling method, while we examine the speedup on ITS, ALIAS, REJ and O-REJ, respectively, when setting the RW as static and dynamic.



(a) Varying number of queries. (b) Varying length of queries. Figure 7: Throughput on *lj* with number and length of queries varying.

Varying number and length of queries. Figure 7a presents the throughput with the number of queries varying from 10^2 to 10^7 . For $10^2 - 10^4$ queries, the execution time is very short and the start up and shut down time can dominate it. For example, for 10^2 queries, each thread spends less than 0.1 ms on performing random walks, while the execution time is around 2 ms because of the cost on resource (e.g., memory and threads) initialization and release. As a result, the benefit of the optimization is limited, and

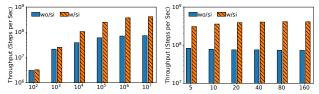
the throughput is lower than that with a large number of queries. The throughput is more than 3×10^8 and keeps stable with the number of queries varying from 10^6 to 10^7 . Figure 7b presents the throughput with the length of queries varying from 5 to 160. The throughput is steady. In summary, ThunderRW has good scalability in terms of the number and length of queries.



Varying number of threads. Figure 8 shows the speedup with the number of threads varying from 1 to 10 (i.e., the number of cores in the machine). For all the five sampling methods on unbiased/static RW, ThunderRW achieves nearly linear speedup with the number of threads as shown in Figure 8a. Particularly, when the number of threads is 10, the speedup is from 8.8X to 9.6X. Figure 8b presents the speedup on dynamic RW. The speedup is from 7.8X to 9.0X. Overall, ThunderRW achieves good scalability in terms of the number of threads.

6.5 Generality Evaluation

To evaluate the generality of ThunderRW, we repeat the first experiment in Section 6.4 on a machine equipped with an Intel Xeon Gold 6246R CPU, which has 16 physical cores. The sizes of L1, L2 and LLC caches are 32KB, 1MB and 35.75MB, respectively. The CPU is based on the *Cascade Lake* microarchitecture, while that used in other experiments is based on *Skylake*. As the CPU has 16 physical cores, we set the number of workers as 16. As shown in Figure 9, enabling the optimization significantly improves the throughput. Moreover, using the new CPU increases the throughput, for example, when the length of queries is 160, the throughput grows from 3×10^8 to 4.1×10^8 . The experiment results show that the techniques proposed in this paper are generic to different architectures.



(a) Varying number of queries. (b) Varying length of queries. Figure 9: Throughput on *lj* with number and length of queries varying on processors with different architectures.

6.6 Discussions

ThunderRW regards a step of a query as a parallel task unit, which parallelizes the computation from the perspective of queries instead of the graph data to exploit the inter-query parallelism. As RW algorithms consist of massive queries and the cost of moving a step is extremely small (e.g., around 34 ns for DeepWalk on *lj*), there are a large number of small parallel tasks, which can be easily parallelized. As such, the parallelization of ThunderRW can achieve significant speedup over the sequential despite that graph structures are complex and flexible. Moreover, the sampling method has an important impact on the performance, and therefore providing variant sampling methods is essential.

The step interleaving technique executes different queries alternately to reduce memory bound incurred by random memory accesses. Its effectiveness is closely related to the memory locality of workloads, which is determined by RW algorithms and graph structures. In general, the optimization tends to achieve higher speedup on large and sparse graphs than small graphs and graphs with dense community structures because RW queries have poorer memory locality on the former graphs. Nevertheless, the random memory access is a common issue for RW algorithms since (1) graphs are much larger than cache sizes; and (2) RW queries wander randomly in the graph. Thus, the step interleaving can achieve significant speedup even on graphs entirely fitting LLC.

However, the speedup achieved by the step interleaving on high order RW algorithms can be lower than that on first order algorithms. First, the operations in user-defined functions can introduce random memory accesses, while the step interleaving technique targets at random memory accesses in the Move operation. Despite that, the optimization still brings 1.2-4.3X speedup on Node2Vec. Second, the Gather operation dominates the cost at each step when performing it in run time because it loops over the neighbors of the current residing vertex of a query.

7 CONCLUSION

In this paper, we propose ThunderRW, an efficient in-memory RW engine on which users can easily implement customized RW algorithms. We design a step-centric model to abstract the computation from the local view of moving one step of a query. Based on the model, we propose the step interleaving technique to hide memory access latency by executing multiple queries alternately. We implement four representative RW algorithms including PPR, Deep-Walk, Node2Vec and MetaPath with our framework. Experimental results show that ThunderRW outperforms state-of-the-art RW frameworks by up to one order of magnitude and the step interleaving reduces the memory bound from 73.1% to 15.0%. Currently, we implement the step interleaving technique in ThunderRW by explicitly and manually storing and restoring states of each query. An interesting future work is to implement the method with *coroutines*, an efficient technique supporting interleaved execution [18, 22, 49].

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