Automated Feature Engineering for Algorithmic Fairness

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ABSTRACT

One of the fundamental problems of machine ethics is to avoid the perpetuation and amplification of discrimination through machine learning applications. In particular, it is desired to exclude the influence of attributes with sensitive information, such as gender or race, and other causally related attributes on the machine learning task. The state-of-the-art bias reduction algorithm Capuchin breaks the causality chain of such attributes by adding and removing tuples. However, this horizontal approach can be considered invasive because it changes the data distribution. A vertical approach would be to prune sensitive features entirely. While this would ensure fairness without tampering with the data, it could also hurt the machine learning accuracy. Therefore, we propose a novel multi-objective feature selection strategy that leverages feature construction to generate more features that lead to both high accuracy and fairness. On three well-known datasets, our system achieves higher accuracy than other fairness-aware approaches while maintaining similar or higher fairness.

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The source code, data, and/or other artifacts have been made available at https://github.com/RicardoSD/FairExp.

1 INTRODUCTION

Algorithms might reinforce biases against groups of people that have been historically discriminated against [45, 46]. Examples include gender bias in machine learning (ML) applications on online advertising [10] and Google image search for occupations [27].

There are two main approaches to address data bias: associational and causal. Associational approaches link the sensitive feature, such as nationality, religion, or race, and the algorithm's outcomes through statistical measures [4, 14, 21]. This approach neglects the influence of sensitive features on other features, leading to paradoxical conclusions [36]. Causal approaches consider a causal structure on the data that allows for causal links between sensitive features, nonsensitive features, the target, and the predictions. Nonetheless, causal approaches typically assume knowledge of the underlying causal structure, which is unrealistic in practice [42]. Therefore, Salimi et al. [42] proposed to let the user categorize features as sensitive, admissible, or inadmissible. The admissible set contains features through which the user allows the influence of the sensitive feature on the classifier's predictions. Conversely, the inadmissible set is composed of features that potentially leak the bias of the sensitive attribute through a mapping. They further propose the system Capuchin (CA), which repairs the data that does not match the user's feature categorization by adding or removing tuples.

Although CA outperforms state-of-the-art (SOA) associational and causal approaches, it has three drawbacks. First, CA overfits fairness. It modifies the training set probability distribution by deleting and inserting tuples and then learns an unbiased classifier to predict unseen instances. The dissimilarities between the probability distributions of the "repaired" dataset used for training and unseen data lead to fairness overfitting. Second, CA's logic requires the binning of numerical features. Depending on the sizes and number of bins, CA might delete more or fewer tuples provoking a loss in classification accuracy. Third, the binning strategy is dataset-dependent, requiring previous knowledge of the problem and the data by the user. Instead of addressing fairness repair with a tuple-wise, i.e., horizontal, approach as CA does, we propose a new approach that addresses the same problem with a feature-wise, i.e., vertical, strategy. A naive solution would drop sensitive and inadmissible features. This approach would successfully remove bias and avoid fairness overfitting, but might hurt the classification accuracy because of potential information loss.

To achieve both high accuracy and fairness, we propose to extract as much unbiased information as possible from inadmissible features using feature construction (FC) methods that apply nonlinear transformations. Thus one can use FC first to generate more possible candidate features and then to drop inadmissible features and optimize for fairness and accuracy. Adapting existing feature generation frameworks [22, 26], we propose a two-phase multiobjective feature selection (FS) strategy that generates a feature set that simultaneously leads to high accuracy and fairness.

Finding a unique feature set that optimizes the trade-off between fairness and accuracy is challenging. By constructing new features, the search space rapidly grows depending on the number of original features. Thus, an exhaustive search, evaluating all objectives on the possible feature combinations, is infeasible. Therefore, a search strategy must consider two potentially competing objectives, and the selection strategy must optimize the trade-off between these objectives. In this paper, we demonstrate a greedy search strategy that fulfills this goal and outperforms SOA preprocessing methods for fairness optimization.

• We show that we can extract unbiased information from biased features by applying human-understandable transformations (Section 3.1). We found that FC through multiplication and group by aggregations are successful for this task.

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- We propose a mixed-initiative approach [23] where our system and the user collaborate to balance the trade-off between accuracy and fairness to the user's needs (Section 3.4).
- We present a series of experiments on known datasets (Section 4) showing how different feature transformations, classification models, feature search space pruning, and weights for fairness and accuracy influence the performance of our approach.

2 FOUNDATION

First, we review general families of bias reduction algorithms. These methods address bias at different stages of the ML pipeline and measure it differently. Finally, we formally define the problem of multi-objective bias reduction.

2.1 Bias Reduction Algorithms

To address algorithmic discrimination, different bias reduction strategies have been discussed and categorized in pre-processing methods, in-processing methods, and post-processing methods.

Pre-processing methods remove the bias by modifying the training data. Since pre-processing methods rely on the training data, they are independent of the ML model. This means that any ML model trained with the resulting training set should show unbiased predictions according to certain fairness criteria. Strategies in this category include cell-mapping of the nonsensitive features by randomized distortions [12], data-augmentation [42], and adversarial learning of feature representations [6, 49]. In-processing methods introduce constraints and regularization terms into the classifier's loss function. Usually, these terms try to moderate the link between the sensitive feature and the algorithm outcomes. For instance, one can add a regularization term to the logistic regression objective's function, penalizing mutual information between the sensitive feature and the predictions [25]. In-processing approaches are model dependent requiring to adjust the constraints and regularization terms depending on the classification model. Post-processing methods modify the outcomes of the classifiers. Strategies include prediction flipping [21] and threshold selection depending on the values of the sensitive attributes [8].

2.2 Measuring Fairness

Several fairness measures have been proposed to capture two legal definitions of discrimination [3]. First, *disparate treatment*, refers to discrimination based on the membership of individuals in a particular group, for instance, neglecting someone's medical treatment because of race. Second, *disparate impact* refers to discrimination in contexts where decisions are not based on sensitive features, and yet they have a larger impact on one or more groups of minorities.

Measures to quantify *disparate treatment* and *disparate impact* can be *associational* or *causal*. Associational measures aim to discover unfair situations through statistical inequalities of the outcomes between the different groups of the sensitive feature. *Demographic Parity (DP), Conditional Statistical Parity,* and *Equalized Odds (EO)* [21] are the most representative measures in this category. Causality approaches analyze whether the classifier's predictions are influenced by the *sensitive feature* through *nonsensitive features* [2]. In contrast to causal approaches, associational approaches are inaccurate in identifying unfair situations in certain cases [42].

According to Salimi et al. [42], *justifiable fairness* is the strongest causal notion of fairness that is testable on data. For a classification task with the features V, the target O, and the sensitive feature S, one can classify the remaining features $V \setminus \{S\}$ as admissible or inadmissible. Through *admissible features*, the user allows an influence of the *sensitive feature* on the outcomes. Unlike other causality-based approaches that assume a fixed causal structure to prohibit paths from the *sensitive feature* to the outcomes [33], the feature categorization proposed by Salimi et al. allows for flexibility regarding the causal structure and it imposes the conditions for an ML model to be *justifiable fair* for these categories. To measure *justifiable fairness*, one can use the *Ratio of Observational Discrimination (ROD)* [42]:

$$\delta(S;O|a_b) = \frac{P(O=1|S=0, A_b=a_b)P(O=0|S=1, A_b=a_b)}{P(O=0|S=0, A_b=a_b)P(O=1|S=1, A_b=a_b)}$$
(1)

where *S* represents the membership to the protected group in the sensitive feature, *O* the outcomes of the model, and *A* the admissible set of features. A_b refers to the subset composed by admissible features influencing the outcomes of the classifier. Formally, $A_b = MB(O) - I$, where MB(O) is the *Markov blanket* of the outcomes, and *I* is the inadmissible set. Modeling the causal relationship of attributes as a direct acyclic graph, the *Markov blanket* comprises the parents, children, and the co-parents of an attribute node. The *Markov blanket* of a node is the minimal set of nodes that isolates the node from the graph - the *Markov blanket* shields the node from the influence of other variables. If $\delta(S; O|a_b) = 1$ then there is no observational evidence that the algorithm discriminates subjects with similar characteristics a_b . If $\delta(S; O|a_b) > 1$ the model potentially discriminates against the sensitive group.

2.3 Problem

We aim to minimize prediction error and algorithmic bias for classification tasks. Given a biased dataset D = (S, A, I), where *S* is the sensitive or protected attribute, *A* is the set of admissible features and *I* is the set of inadmissible features, we aim to enrich the feature vector in a way that a subset $X \subseteq V$, where *V* is the set of constructed features from $A \cup I \cup S$, minimizes algorithmic bias and prediction error for an algorithm mapping *X* to an outcome *O*.

We adopt the causal perspective of *justifiable fairness* and use the *Ratio of Observational Discrimination (ROD)* $\delta(S; O|a_b)$ as the objective function $g_1 = |1 - \delta(S; O|a_b)|$ to minimize algorithmic bias. Moreover, we use the F1 score as the objective function g_2 to minimize prediction error. The F1 score is defined as $F1 = 2 \times \frac{(P \times R)}{(P+R)}$, where precision (P) is the fraction of correctly positive classified instances and recall (R) is the fraction of the truly positive classified instances that are discovered. Given the objective functions $g_1(X)$ and $g_2(X)$, the optimization problem can be written as:

maximize
$$G([-g_1(X), g_2(X)]).$$
 (2)

3 AUTOMATED FAIR FEATURE ENGINEERING

Figure 1 illustrates the workflow of FAIREXP (FAIRNESS EXPLORER), which transforms a biased dataset D into a bias-reduced dataset D'. First, the user provides D and specifies the sensitive and inadmissible features. Optionally, the user can provide weights for the

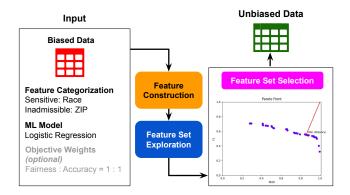


Figure 1: System Workflow.

Table 1: Std(workclass = Local-gov) GroupyBy marital-status

Class	Sex	Std(workclass == "Local-gov") GroupBy marital-status
<=50K	Female Male	0.24 ± 0.03 0.24 ± 0.02
>50K	Female Male	$\begin{array}{c} 0.25 \pm 0.02 \\ 0.25 \pm 0.01 \end{array}$

objectives accuracy and fairness. The workflow consists of three main steps: FC, feature set exploration, and feature set selection. FAIREXP constructs new features from the original features by recursively applying transformations. FC enables the extraction of unbiased information even from biased features as we describe in Section 3.1. Note that we do not prune any biased features in the construction phase.

In contrast to existing work, which applies simultaneous optimization of accuracy and fairness [11] and can run into a local minimum, we propose a two-phase exploration strategy. Having in mind that smaller and less complex feature sets generalize better, we first try to find the minimal set of features that maximizes accuracy. For this purpose, we propose a definition of feature set DL that serves our purpose. In the second phase, we trim the feature set to fulfill the fairness requirement, as we explain in Section 3.2. The exploration yields a broad candidate set of possible feature sets in the Pareto front trading off accuracy and fairness. As detailed in Section 3.4, we apply a geometric solution similar to the "elbow method" [5] to pick the optimal feature set while considering the objective weighting if specified. Finally, we return the preprocessed, bias-reduced dataset to the user.

3.1 Feature Construction

To reduce bias one has to avoid inadmissible features. However, if we drop all inadmissible features, we lose too much information. So, the idea is to use some information about inadmissible features by leveraging information from unbiased relationships with other features. Salimi et al. [41] showed that the Adult dataset is inconsistent because it reports household incomes for married individuals, and there are more male married individuals in the sample. Thus, the categorical feature *marital-status* is considered inadmissible because it could bias the outcomes in favor of married males. However, as observed from Table 1, the feature *Std(workclass*) == "Local-gov") GroupyBy marital-status is not biased towards a specific sex and benefits the classification accuracy. To obtain features, such as Std(workclass == "Local-gov") GroupyBy marital-status, we apply transformations to the original features recursively.

FAIREXP constructs new features to increase the classification accuracy by applying transformations on the original features. We leverage the same set of transformations as proposed by Katz et al. [26]. The standard operations +, *, 1/, -1*, and *log* model arithmetic relationships among features. The encoding transformations equal-range discretization, min-max scaling, and one-hot encoding facilitate learning for ML models. The partial aggregates GroupyByThen{Min, Max, Mean, Standard Deviation} allow FAIR-EXP to model conditional relationships among features.

Theoretically, we can apply infinitely many transformations recursively. However, we stop once a feature reaches a certain description length (DL). Inspired by the *Minimum Description Length* (MDL) principle [39], we recursively define the DL of a feature:

$$DL(\{f_m\}) = 1, f_m \in F_0,$$
(3)

$$DL(F_a) = \sum_{f_m \in F_a} DL(f_m), \tag{4}$$

$$DL(\{F_a, F_b\}) = DL(F_a) + DL(F_b),$$
(5)

$$DL(\{t(F_a)\}) = DL(F_a) + 1, t \in T,$$
(6)

where
$$F_a, F_b$$
 are any feature set. (7)

For instance, we would consider a raw feature A to have DL 1. For every transformation that we apply, we increment the DL accordingly. E.g. log(A) has DL 2 and Max(A) GroupBy B has DL 3.

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Instead of generating all possible combinations of features (brute force) and transformations for the specified DL level, we leverage a linear algebra solver [32] to avoid generating algebraically equivalent features, such as the commutative property a + b = b + a, distributive property, e.g., $(a \cdot b) + (a \times c) =$ $a \cdot (b + c)$, associative property, e.g., (a + b) + c = (b + c) + c*a*, idempotent property, e.g., MinMaxScaling(MinMaxScaling(*a*)) = MinMaxScaling(a), input-dependent idempotent property, e.g. $\max(\max(a) \text{ Group By } b) \text{ Group By } b = \max(a) \text{ Group By } b$, and invertibility property, e.g. $a/b \cdot b = a$. Additionally, we prune all constant features, e.g. a/a = 1. Despite these optimizations, there is still an exponential growth of the feature space. For instance, in the German Credit dataset with 21 raw features (DL 1), we would still face 1k features of DL 2, 1.8k features of DL 3, and 7.5k features of DL 4. In Section 3.5, we describe how we parallelize our algorithm to quickly cover thousands of constructed features.

3.2 Two-Phase Feature Set Exploration

Algorithm 1 describes in detail how we gather the most promising candidate feature sets in a two-phase approach. We search for feature sets that contain few and simple features. First, we add features that benefit accuracy to find the least complex model that maximizes accuracy and then we remove biased features.

Algorithm 1 takes a dataset D, the user-specified feature categorization, the model, and the constructed features C as input. In the first phase (Lines 4 - 11), the algorithm iteratively adds constructed features to an initially empty feature set F as long as they improve accuracy on a validation set. Note that the constructed features are sorted by increasing DL - starting with the raw features and ending

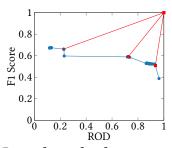


Figure 2: The Pareto front after feature set exploration. Selecting feature set with fairness weight of 0.25, 0.5, and 0.75.

with the features that are the result of more complex transformations. This way our system prefers simple features, which are easier to understand by users, over complex ones. We further enforce this principle by applying the floating procedure [38] (Lines 8 -11) to further reduce the size of the resulting feature sets. Floating removes redundant features from the current feature set if possible without harming the accuracy. After evaluating all constructed features, phase 1 yields one large feature set with the highest validation accuracy. The complexity of the first phase is theoretically exponential but capped by the specified description lengths. Given n raw features and m operations and a cap of l as the maximum description length. The number of possible feature combinations are all the combinations of single raw features and permutations of raw features and operations of higher ranks: $O(n + \sum_{i=2}^{l} (n+m)^{i})$. In phase 2, we start with this accurate feature set and incrementally remove one feature at a time if it improves fairness. Each time that we remove a feature, we apply floating. Here, floating means that we verify whether adding one of the removed accurate features benefits fairness of the current feature set. If that is the case, we add it to the feature set again. Floating is necessary because fairness is a non-monotonic measure and therefore removing one feature might significantly affect the properties of the underlying feature set. The second phase terminates once every feature in the set F has been considered for removal. The complexity of the second phase is $O(|F|^2)$ where |F| is the number of the features that were found in the first phase. Therefore, the complexity of the entire algorithm is dominated by the first phase because usually $|F| \ll |C|$.

From all explored feature sets, we select those on the Pareto front. In the next section, we discuss how to choose one feature set from the candidates in this Pareto front.

3.3 Fairness Guarantee

The feature subset obtained after the first phase of Algorithm 1 might contain biased features. Improving ROD in the second phase of Algorithm 1, removes features with a direct influence on the outcomes but not necessarily provides a fairness guarantee. To guarantee that there are no hidden correlations between the sensitive features and the target, in addition to the condition in Line 14, we check whether the given features have any violating correlation. We apply the SeqSel [19] algorithm proposed by which uses conditional independence tests [47] to remove features that leak sensitive information and are not blocked by the admissible feature set. Ghalotra et al. also prove that SeqSel ensures causal fairness

Algorithm 1 Two-Phase Feature	Set Exploration
Input: dataset <i>D</i> , feature categorization, m	nodel, constructed features C.
Output: evaluated feature subsets <i>O</i> .	
1: $C \leftarrow$ the list of all constructed features 2: $F \leftarrow \emptyset$	b the current feature subset
$\begin{array}{c} 2: \ P \leftarrow \emptyset \\ 3: \ O \leftarrow \emptyset \end{array}$	Ine current leature subset
Phase 1: Exploration for accurate featu	ıre sets
4: for c in C do	
5: if $F1(F \cup c) > F1(F)$ then	
$6: \qquad F \leftarrow F \cup c$	
7: $O \leftarrow O \cup (F, F1(F), ROD(F))$)
8: for f in F do	▶ floating
9: if $F1(F \setminus f) > F1(F)$ then	1
10: $F \leftarrow F \setminus f$	
11: $O \leftarrow O \cup (F, F1(F), Re$	OD(F))
Phase 2: Exploration for fair feature se	ets
12: $B \leftarrow \emptyset$	▹ the set of potentially biased features
13: for <i>f in F</i> do	
14: if $ROD(F \setminus f) > ROD(F)$ then	
15: $F \leftarrow F \setminus f$	
16: $O \leftarrow O \cup (F, F1(F), ROD(F))$)
17: $B \leftarrow B \cup f$	
18: for <i>b in B</i> do	⊳ floating
19: if $ROD(F \cup b) > ROD(F)$) then
20: $F \leftarrow F \cup b$	
21: $O \leftarrow O \cup (F, F1(F), Re$	OD(F))
22: $O \leftarrow Pareto Front(O)$	

even if some features in the subset capture information about sensitive features [19].

3.4 Mixed-Initiative Feature Set Selection

Accuracy and fairness are two competing objectives. Therefore, all explored feature sets in the Pareto front are potential solutions for the ML application. Following the mixed-initiative approach [23] where our system and the user collaborate to achieve the user's goal, we propose three increasing levels of autonomy - supervised, semi-supervised, and unsupervised.

Supervised. The user has a clear understanding of which degree of fairness is required for the given ML application. Therefore, the user can pick the feature set from the Pareto front by choosing the most accurate feature set that still satisfies the fairness constraint. **Semi-Supervised.** The user specifies the trade-off between accuracy and fairness by specifying weights for each objective. Based on the weights, FAIREXP automatically chooses the feature set that fits the user-specified trade-off best. FAIREXP chooses the feature set with the maximal weighted sum of both objectives:

$$z = \underset{x \in \mathcal{P}}{\operatorname{argmax}} w_{\text{fair}} * ROD + (1 - w_{\text{fair}}) * F1 \text{ score}, \tag{8}$$

where \mathcal{P} contains all feature sets in the Pareto front and w_{fair} is the weight for the fairness objective. This approach resembles the "elbow method" [5] that was proposed to find the optimal number of clusters for unsupervised learning problems. For instance, Figure 2 illustrates how FAIREXP selects the feature set from the Pareto front for the Adult dataset based on the fairness weights 0.25, 0.5 (equal weights), and 0.75. In Section 4.5.2, we show the impact of considering different weighting schemes in the selected feature set. **Unsupervised.** FAIREXP chooses the feature set automatically based on the assumption that both objectives are equal and the weights of both objectives are set to 0.5.

Table 2: Experimental datasets.

Dataset	Columns	Rows	Sensitive	Inadmissible
Traffic	17	1M	Race	-
Adult	10	48k	Gender	Marital status
COMPAS	5	7k	Race	-
German Credit	21	1k	Age	-

3.5 Scalability

Feature engineering consists of FC and FS. To scale feature engineering, one has to optimize both stages. The bottleneck of feature engineering is the exponentially growing number of constructed features. To reduce this exponential growth, multiple strategies have been proposed. First, our approach prunes all algebraically equivalent features, such as a + b = b + a. Second, one can always parallelize parallelizable parts of the algorithm. For instance, we currently compute the features of the FC phase in parallel. Furthermore, we also parallelize the evaluation of one feature set. For instance, for some models, such as logistic regression, we can distribute the training to multiple cores (training parallelism). As we apply 5-fold cross-validation (CV), one can also compute each fold in parallel (CV parallelism). However, for CV parallelism the upper bound is the number of folds. Besides these trivial approaches to parallelize Algorithm 1, we analyzed the algorithm more closely and found two further parallelization opportunities. First, one approach is to parallelize the for loop of the floating procedure in Line 8. Second, we can also accelerate the forward pass of Algorithm 1 by leveraging additional compute resources. Inspired by branch prediction [44], we can speculatively evaluate additional potential feature sets to utilize all resources. As FC generates a large number of features and most of these features do not yield a gain in model accuracy, we can assume that the condition in Line 5 yields False in most cases and we can already evaluate the feature sets of the next k iterations where k is the number of cores. In the best case, we can evaluate the feature sets of k iterations in one cycle. In the worst case, we have no parallelism gain.

4 EXPERIMENTS

We performed several experiments to compare our approach against the SOA. We compare our approach in terms of prediction quality, fairness, and runtime. Also, we explore the impact of different feature evaluation methods, objective weighting, including features with longer DL, increasing number of instances, inadmissible features. Finally, we analyze our parallelization strategy.

4.1 Experimental Setup

4.1.1 Datasets. We conducted our experiments on three commonly studied datasets in algorithmic fairness literature [7, 12, 17, 42]. Moreover, we use the Traffic dataset [9] to analyze the runtime performance of our approach for an increasing number of instances. Table 2 summarizes the datasets along with the number of columns, rows, sensitive features, and inadmissible features if present.

The Adult dataset [13] contains information from the 1994 census in the United States. The prediction task is to determine whether a person makes over 50K dollars a year. Similar to prior work [42], we consider the sex (male, female) as the sensitive feature and marital status as an inadmissible feature because as pointed out in prior literature marital status is highly biased towards males. To compare with prior work [12, 42], we remove the features that contain other sensitive information such as race, native-country, and relationship.

The COMPAS dataset [30] contains records of offenders. The prediction task is to determine if an offender will relapse before trial. The dataset displays 1.5 times more African-Americans than Caucasians. Following prior work [42], we consider race as the sensitive feature, and the remaining features (age, number of prior convictions, and severity of charge degree) as admissible.

The German Credit dataset [13] contains financial information of credits granted to individuals in Germany. The prediction task is to classify whether a person will pay back the credit or not. We consider age as the sensitive feature (below average, above average).

The Montgomery County Traffic violations dataset [9], contains electronic traffic violations. The classification task is to predict whether the traffic violation corresponds to a warning or a citation. Moreover, the data shows that citations are issued in a significantly larger proportion to Hispanics when compared to other races.

4.1.2 Methods. We compare our method to the following methods. **Original.** We leverage the original complete feature set.

Dropped. This baseline corresponds to the original feature set without the sensitive and inadmissible features, which are dropped. **CA** [42]. We bin the numerical features as proposed by the authors. **Kamiran.** We use the sample reweighting method proposed by Kamiran et al. [24]. **Calmon.** We use the same binning, feature subset, and distortion function as reported for the Adult and COM-PAS datasets [12]. For the German credit dataset, we only consider numerical and ordinal features as it is required for this method. **Feldman.** We use the same binning and feature subset reported by Calmon et al. [12] for the adult dataset. For the German credit dataset, we only consider numerical and ordinal features as it is required for this method.

FC-NSGA-II. To evaluate a SOA multi-objective FS, we use the Non-dominated Sorting Genetic Algorithm (NSGA-II) [11] on the constructed features. Khan et al. [28] proposed to use feature set size and accuracy as objectives for selecting features using NSGAII. FAIREXP. For our system, we use by default a maximum feature DL of 4. Moreover, we assign equal weights (0.5) to fairness and accuracy objectives. For our feature evaluation component, we use logistic regression with 3-fold cross-validation on the training set to compute a validation score.

4.2 Evaluation Methodology

We measure the effectiveness of our methods by comparing the F1 score (as defined in Section 2.3) and the discrimination reduction using the *Ratio of Discrimination (ROD)* and all other fairness metrics reported by Salimi et al. [42] of the downstream classification task. F1 score is suitable in cases of class imbalance and ROD represents the strongest notion of fairness that is testable from data [42]. Following prior work [42], we normalize the distance to the best possible ROD score (d = |1 - ROD|) between 0 and 1, where 1 represents the best possible fairness. Accordingly, we also use the Grow-shrink algorithm [31] to learn the *Markov blanket* of the outcomes to compute the ROD score. We report the aggregated result of 5-fold cross-validation.

Table 3: Comparing FAIRExP to state-of-the-art and baselines with regard to downstream F1 score and fairness measures

Dataset	Method	F1	ROD	DP	TNB	TPB	CSP	CTNB	CTPB	Runtime
	Capuchin	61 ± 1	82 ± 5	84 ± 5	84 ± 3	70 ± 13	96 ± 3	94 ± 5	96 ± 3	69.89 ± 20
	Dropped	61 ± 1	87 ± 4	75 ± 5	77 ± 6	72 ± 5	87 ± 1	88 ± 2	57 ± 6	9.43 ± 54
	FairExp	64 ± 3	81 ± 29	76 ± 32	82 ± 36	86 ± 21	66 ± 30	66 ± 30	40 ± 11	$163k \pm 51k$
Adult	FairExp-guaranteed	62 ± 2	85 ± 4	74 ± 6	78 ± 6	66 ± 6	86 ± 1	87 ± 2	54 ± 5	$96k \pm 31k$
Adult	FC-NSGAII	70 ± 1	16 ± 8	12 ± 4	42 ± 6	14 ± 3	10 ± 4	11 ± 7	13 ± 3	$61k \pm 38$
	Kamiran-reweighting	63 ± 0	85 ± 7	96 ± 4	88 ± 3	71 ± 13	60 ± 4	62 ± 4	47 ± 5	9.44 ± 18
	Original	68 ± 1	22 ± 5	7 ± 5	4 ± 4	27 ± 8	4 ± 4	4 ± 4	10 ± 7	8.95 ± 15
	Capuchin	64 ± 1	98 ± 2	42 ± 9	62 ± 14	42 ± 13	95 ± 10	96 ± 10	95 ± 10	1.82 ± 17
	Dropped	66 ± 3	89 ± 2	38 ± 15	61 ± 17	36 ± 15	89 ± 4	85 ± 7	85 ± 5	1.21 ± 11
	FairExp	67 ± 2	91 ± 4	46 ± 11	58 ± 16	52 ± 17	88 ± 6	84 ± 7	88 ± 7	95.97 ± 22.8
COMPAS	FairExp-guaranteed	66 ± 3	78 ± 21	33 ± 20	58 ± 18	30 ± 23	74 ± 24	71 ± 21	72 ± 21	149.24 ± 9.0
COMPAS	FC-NSGAII	65 ± 3	68 ± 18	26 ± 22	38 ± 22	33 ± 17	54 ± 35	49 ± 37	62 ± 22	$1k \pm 18$
	Kamiran-reweighting	65 ± 2	4 ± 5	85 ± 13	90 ± 10	87 ± 11	33 ± 10	26 ± 16	36 ± 4	1.27 ± 12
	Original	66 ± 3	52 ± 8	19 ± 16	45 ± 19	15 ± 17	56 ± 12	62 ± 16	54 ± 9	1.13 ± 10
	Capuchin	83 ± 3	80 ± 13	49 ± 31	66 ± 30	59 ± 31	0 ± 0	0 ± 0	0 ± 0	13.61 ± 3.0
	Dropped	78 ± 4	83 ± 18	59 ± 10	76 ± 31	72 ± 30	0 ± 0	0 ± 0	0 ± 0	1.24 ± 15
	FairExp	81 ± 3	1.00 ± 0	91 ± 7	78 ± 20	94 ± 6	0 ± 0	0 ± 0	0 ± 0	$1k \pm 391.7$
German credit	FairExp-guaranteed	78 ± 3	67 ± 29	38 ± 27	64 ± 29	49 ± 30	0 ± 0	0 ± 0	0 ± 0	$4k \pm 2665$
German credit	FC-NSGAII	79 ± 5	57 ± 34	38 ± 26	45 ± 30	66 ± 29	0 ± 0	0 ± 0	0 ± 0	$10k \pm 167$
	Kamiran-reweighting	83 ± 3	80 ± 27	87 ± 10	60 ± 24	80 ± 19	0 ± 0	0 ± 0	0 ± 0	1.33 ± 9
	Original	78 ± 3	70 ± 12	32 ± 19	71 ± 20	50 ± 35	0 ± 0	0 ± 0	0 ± 0	1.31 ± 14

4.3 Effectiveness

Table 3 reports for each competing method the mean and standard deviation of achieved F1 and various fairness scores across different datasets. We bold the first and second-best results for each score. The results show that FAIREXP is competitive compared to all SOA baselines. Leveraging the original complete feature set yields high classification accuracy but poor fairness because bias is not considered. If we remove sensitive and inadmissible features from the original feature set, we significantly improve fairness but also cause a significant drop in classification accuracy as can be seen for the baseline Dropped. In addition to removing biased features, the SOA strategy CA further reduces bias in the data horizontally by adding and removing instances. However, the disadvantage of CA is that its horizontal bias repair significantly changes the underlying distribution of the training set which leads to it overfitting for fairness and less generalization for the unseen test set. Furthermore, CA requires discretization of numerical features that might cause an additional loss in information depending on the degree of binning.

The multi-objective FS strategy NSGA-II achieves high classification accuracy and low fairness. We found that NSGA-II often gets stuck in local optima due to the large number of features. Therefore, it tends to prefer one objective over the other. Another reason why FAIREXP outperforms NSGA-II is that NSGA-II does not consider the DL of constructed features and, therefore, might overfit.

To better showcase the approach of FAIREXP, consider the following features that were generated and selected. For instance, the following features are constructed and selected for the Adult dataset instead of using the inadmissible feature marital-status: mean(maritalstatus = "Divorced") GroupBy capital-loss, mean(marital-status = "Widowed") GroupBy capital-loss, and std(workclass = "Local-gov") GroupBy marital-status. These features show an equal distribution with regard to the different groups inside the sensitive attribute Sex and add predictive power for the classification model. By considering only specific values of marital-status and combining it with other features, we can extract unbiased information that leads to higher accuracy. On German Credit, the sensitive feature age was combined with the feature *existing credits* to extract additional information: *mean(age = "above average") GroupBy existing credits.*

For COMPAS, our method did not select features that captured data from the sensitive feature *race*. Instead, the following features were considered: (*max*(*age* = "Less than 25") GroupyBy priors count), *age* = "Greater than 45" * priors count.

To compare our system to Calmon et al. [12] and Feldman et al. [17], which are designed for numerical ordinal features, we removed all non-numerical and non-ordinal features.

Table 4 shows that FAIREXP performs poorly for this case because the number of features is very low, e.g. only *age* and *education* for Adult. Therefore, FAIREXP cannot uncover any meaningful relationships between features using FC. All in all, the experiment shows that FAIREXP is a promising alternative to SOA bias reduction approaches that follows a vertical approach.

4.4 Runtime

Table 3 reports the runtime in seconds for all described methods. We define runtime as the total elapsed time that a method takes to complete the pre-processing component (FC, feature exploration, and feature set selection) of a system, and to train the model with the selected representation. All strategies that leverage FC, such as FC-NSGA-II and FAIREXP, require multiple orders of magnitude more time than strategies that do not. There is a trade-off between runtime and effectiveness. However, we accelerate our approach by parallelizing the algorithm as described in Sec. 3.5.

4.5 Micro-Benchmark Results

We present an analysis of the influence of different FC parameters and representation selection components on accuracy, fairness, and runtime. Moreover, we conduct an experiment to show which FC transformations are most likely to remove bias from input features.

4.5.1 *Feature Construction.* Theoretically, we can apply transformations arbitrarily many times recursively. To reduce the runtime of FC, we have to limit the number of constructed features. Table 5 shows how choosing different degrees of DL, as defined in

Dataset	Method	F1	ROD	DP	TNB	TPB	CSP	CTNB	CTPB	Runtime
	Calmon	49 ± 01	70 ± 02	92 ± 03	79 ± 07	86 ± 13	1.00 ± 00	94 ± 03	71 ± 07	725.21 ± 19.57
Adult	Capuchin	41 ± 01	90 ± 12	92 ± 06	95 ± 07	87 ± 10	1.00 ± 00	1.00 ± 01	99 ± 01	5.38 ± 1.70
Adult	FairExp	57 ± 01	32 ± 19	25 ± 23	47 ± 40	57 ± 32	25 ± 22	29 ± 24	29 ± 19	744.90 ± 295.40
	Feldman	45 ± 01	$\textbf{1.00}\pm00$	81 ± 03	86 ± 06	87 ± 11	$\textbf{1.00} \pm 00$	$\textbf{1.00}\pm00$	90 ± 18	3.58 ± 07
	Calmon	66 ± 01	38 ± 34	55 ± 31	54 ± 32	49 ± 27	80 ± 45	80 ± 45	80 ± 45	116 ± 1.14
COMPAS	Capuchin	64 ± 01	78 ± 10	53 ± 15	64 ± 24	35 ± 22	92 ± 17	92 ± 17	92 ± 17	1.82 ± 17
COMPAS	FairExp	68 ± 02	48 ± 29	56 ± 13	59 ± 17	44 ± 23	78 ± 17	67 ± 18	77 ± 12	102.83 ± 17.32
	Feldman	65 ± 01	$\textbf{1.00} \pm 01$	91 ± 06	85 ± 11	82 ± 13	85 ± 13	80 ± 09	78 ± 12	2.60 ± 07
German credit	Calmon	82 ± 02	61 ± 50	89 ± 09	85 ± 13	92 ± 09	96 ± 07	92 ± 11	66 ± 24	1536 ± 1.93
	Capuchin	82 ± 04	39 ± 28	39 ± 30	40 ± 35	59 ± 42	53 ± 36	41 ± 31	51 ± 35	8.17 ± 1.47
	FairExp	76 ± 06	97 ± 02	86 ± 15	85 ± 13	84 ± 14	98 ± 04	93 ± 07	88 ± 08	604.68 ± 28.10
	Feldman	82 ± 02	90 ± 09	86 ± 07	74 ± 21	90 ± 04	99 ± 03	1.00 ± 00	79 ± 12	3.28 ± 1.44

Table 4: Comparison on datasets with numerical and ordinal features only

Table 5: Impact of DL on accuracy, fairness, and runtime.

Dataset	DL	Const. features	F1	ROD	Runtime
	1	0	44 ± 1	98 ± 1	29 ± 1
Adult	2	432	56 ± 1	95 ± 2	$1.2k \pm 178$
Adult	3	647	60 ± 1	93 ± 2	$5.9k \pm 931$
	4	3.4k	62 ± 3	91 ± 3	$50.5k \pm 4.2k$
	1	0	46 ± 3	92 ± 4	6 ± 1
COMPAS	2	21	46 ± 3	93 ± 4	18 ± 3
COMPAS	3	61	46 ± 3	93 ± 4	76 ± 15
	4	199	55 ± 2	78 ± 10	$5.6k \pm 2.2k$
	1	0	55 ± 31	96 ± 3	15 ± 2
German	2	1k	77 ± 5	97 ± 4	190 ± 11
Credit	3	1.8k	83 ± 3	91 ± 5	$7.7k \pm 109$
	4	7.5k	80 ± 2	89 ± 8	$8.5k \pm 526$

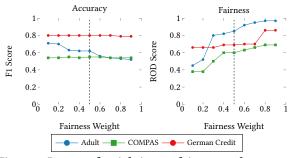


Figure 3: Impact of weighting on fairness and accuracy.

Section 3.1, affects accuracy and fairness. With increasing DL, the number of constructed features grows exponentially because new features can be combined with old and new features to create even more features. This exponential growth also affects the runtime significantly. However, with increasing DL, the classification accuracy improves because we can extract more and more information from the original features. At the same time, fairness slightly decreases but maintains a high level. Therefore, we construct features until a DL of 4 because, this way, we achieve high accuracy while maintaining competitive fairness. Constructing features with DL higher than 4 is not feasible because the runtime increases exponentially. To generate features of DL 5, more than a week of computation time can be expected for each dataset.

4.5.2 *Objective Weighting*. Depending on the use case, fairness might be more important than accuracy and vice-versa. Therefore, in our system, users can specify this trade-off. In this experiment, we evaluate the impact of different weighting schemes. Figure 3

Table 6: Comparison	ı of different	classification	models.
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	Adult		COI	MPAS	German Credit		
Model	F1	ROD	F1	ROD	F1	ROD	
LR	62 ± 3	91 ± 3	55 ± 2	78 ± 10	80 ± 2	89 ± 8	
SVM	55 ± 9	70 ± 21	37 ± 7	79 ± 8	82 ± 2	85 ± 11	
GB	55 ± 9	64 ± 20	41 ± 5	41 ± 10	80 ± 2	58 ± 20	

Table 7: Scaling the number of rows for the Traffic dataset.

Number Rows	1k	10k	100k	1M
Runtime (seconds)	168 ± 12	463 ± 70	2984 ± 1098	20670 ± 2293

shows the impact of different weighting schemes for our strategy FAIREXP on the evaluated datasets.

As observed in Figure 3, the fairness score improves as the weight for the fairness objective increases. However, for German Credit and COMPAS, the accuracy stays relatively stable even with increasing weight for fairness. The reason is that, for these two datasets, there are very few important and unbiased features. Therefore, removing additional features does not significantly affect the classification accuracy. The opposite is true for Adult where many features are required to achieve high accuracy. Therefore, we see a decline in accuracy when increasing the fairness weight because more and more features will be removed.

4.5.3 Model Selection. We analyze the influence of the classification model on the optimization problem. We experimented with 3 different models: gradient boosting (GB), logistic regression (LR), and support vector machines (SVM). Table 6 shows the accuracy and fairness for three models across the three benchmark datasets. In general, the scores vary across models. For instance, GB achieves a lower ROD score compared to the other two models. The reason is that GB on its own also selects features in its training phase to optimize accuracy. This focus on accuracy affects the fairness score negatively. Generally, it is well-known that different ML models fit different datasets differently well, which motivates the field of algorithm selection [18].

4.5.4 *Scalability*. In Section 4.5.1, we already analyzed the scalability across the number of constructed features. We now evaluate the scalability of our approach with respect to the number of instances and the number of inadmissible features. Table 7 shows that our approach scales linearly for an increasing number of instances.

Second, we experimented on a randomly generated dataset with 2000 rows and 198 boolean features, one target, and one sensitive

Table 8: Scaling the number of inadmissible features.								
# Inadmissible Features	1	10	25	50				
Runtime (s)	365 ± 41	376 ± 61	393 ± 36	340 ± 11				

Training	CV	Speculative	Runtime (s)
Parallelism	Parallelism	Parallelism	German Credit	Traffic
1	1	1	6359	391
27	1	1	6703	389
1	5	1	7082	339
1	1	27	1228	175

Table 10: Different ranking strategies on Adult

Ranking Strategies	F1	ROD
MDL	0.61	-0.707
reverse MDL	0.62	-0.716
Random	0.61	-1.456

Table 11: Capuchin and FAIREXP

	Adult		COMPAS	
Method	F1	ROD	F1	ROD
Original CA CA-FAIREXP CA-FAIREXP-Dropped FAIREXP	$68 \pm 1 62 \pm 1 53 \pm 5 56 \pm 1 60 \pm 2$	$17 \pm 14 77 \pm 3 92 \pm 6 93 \pm 5 92 \pm 5 92 \pm 5$	$66 \pm 1 64 \pm 1 65 \pm 2 66 \pm 2 67 \pm 2$	7 ± 10 94 ± 3 79 ± 15 83 ± 20 80 ± 7

feature. Then, we randomly pick an increasing number of inadmissible features. Table 8 contains the results of this experiment. It shows that the number of inadmissible features only marginally affects runtime because we have to conduct the same number of conditional independence tests. Computationally, we treat sensitive features and inadmissible features the same. Therefore, increasing the number of sensitive features behaves the same way as increasing the number of inadmissible features.

4.5.5 *Parallelization.* Table 9 compares training, CV, and speculative parallelism. For German Credit, training and CV parallelism introduce too much overhead and therefore require even more runtime than running without parallelism. Only the parallelization approach that speculatively evaluates feature sets is 5 times faster than without parallelization by leveraging 27 CPU cores. However, when running on a larger dataset, e.g. Traffic with 10k examples, training and CV parallelization improve the runtime compared to no parallelization.

4.5.6 *Ranking Strategies.* In the forward pass of Algorithm 1, we rank the features first based on their DL. Table 10 compares the ranking strategies MDL, reverse MDL, and random. All of them achieve similar results. Therefore, we chose MDL as it prefers simple features over complex ones.

4.5.7 Combining horizontal and vertical bias reduction. We first bin the data, repair it using CA. Then, we apply FAIREXP on the repaired data (use the original data points as opposed to the binned ones for those that are retained by the repair algorithm). Table 11 shows the result of this experiment. FAIREXP improves the fairness because CA guarantees fairness on training but overfits. FAIREXP achieves higher fairness by optimizing for the cross-validation score. The results are similar when we additionally drop sensitive and inadmissible attributes (CA-FairExp-Dropped).

5 RELATED WORK

Our work is strongly related to research on algorithmic bias reduction and feature engineering.

Algorithmic Bias Reduction. Recent work for reducing bias includes pre-processing [1, 12, 17, 50], in-processing [29, 33, 37, 40, 43] and post-processing [21, 48] strategies. Pre-processing methods aim to remove the bias in the training data either by modifying the probability distributions [12, 17, 50], selecting a subset of features [19], or defining different feature weight strategies [1]. In-processing methods impose constraints on the algorithm's loss function [25] and optimize fairness by tuning the classifier's hyperparameters [37]. Post-processing methods aim to remove the bias via some transformation of the predictions [8, 21]. Our algorithm follows the pre-processing approach but does not only optimize for accuracy but also fairness.

Furthermore, bias reduction algorithms either follow an associational or a causal approach to measure fairness. Associational approaches check for inequalities in the algorithm's outcomes between groups of the sensitive feature, while causal strategies aim to identify, quantify, and remove the influence of the sensitive feature on the outcomes. Approaches based on causality frameworks [12, 42] have shown to avoid paradoxical conclusions and provide more principled reasoning to understand the influence of the sensitive features on an algorithm's outcome [42]. Our solution follows the spirit of the described causal algorithmic fairness frameworks but none of them employs FS and FC simultaneously to address the problem with a multi-objective approach.

Feature Engineering. Feature engineering has been used to improve prediction performance, provide faster and more cost-effective predictors, and provide a better understanding of the underlying process generating the data [15, 16, 20, 26, 34]. Feature engineering approaches have been lately proposed for algorithmic fairness [35].

6 CONCLUSION

We proposed a novel pre-processing bias reduction algorithm based on automatic FC and selection that does not only optimize for accuracy but also fairness. Our system generates a large number of new features from the original feature set by applying humanunderstandable transformations. Our experiments show that our system achieves competitive results compared to SOA strategies. Unlike SOA, our method does not require the deletion of tuples and, therefore, it generalizes better to unseen data. Further research is needed to efficiently restrain the large number of feature candidates and explanation of constructed features.

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