CERTIFICATION BY INTERVALS OF TIMESTAMPs
IN DISTRIBUTED DATABASE SYSTEMS

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Abstract
This paper introduces, as an optimistic concurrency control, a new certification method by means of intervals of timestamps, usable in a distributed database system. The main advantage of this method is that it allows a chronological validation order which differs from the serialization one (thus avoiding rejections or delays of transactions which occur in usual certification methods or in classical locking or timestamping ones). The use of the dependency graph permits both classifying this method among existing ones and proving it.

1. INTRODUCTION
Numerous Concurrency Control Methods (CCMs) for Distributed Data Bases (DDBs) have been proposed so far [Bernstein 81] using either Two-Phase Locking (2PL) or Timestamp Ordering (TO).

The main feature of these CCMs is that the serializability test is made for each action (Read or Prewrite) on an object of the base. For this reason, we call these CCMs continuous ones as opposed to certification (also called optimistic) ones, where the serializability test is only made at the end of the transaction.

Usually, continuous CCMs and certification ones are described in totally different ways. Our study offers a unifying view for this classification.

Certification methods [Kung 81], [Haerder 82], [Lausen 82] have been studied mostly for centralized systems. The few proposals adapted to distributed systems [Badal 79], [Schlageter 81], [Bhargava 82] are not convincing due to lack of formal proofs for their desired behavior. We answer that problem by proving a certification method in a distributed system.

Serialization control used in CCMs relies on the setting of a serialization order among transactions. In continuous CCMs two principles are used to construct this order. In 2PL methods [Traiger 82], it is dynamically constructed and corresponds to the order into which transactions reach their maximum locking point. The well known drawback of these methods is useless waiting sometimes imposed to transactions and deadlocks which may occur. Deadlock prevention may be applied [Rosenkrantz 78] at the cost of increasing the number of rejections. In basic or multiversions TO CCMs, the order is "static" and relies upon the giving of a unique timestamp to any transaction, thus defining the serialization order. One study [Bayer 82] refines this technique by introducing the notion of a "dynamic" timestamp which avoids useless rejection of a transaction when its first conflict arises, in a very particular CCM.

Control by certification allows a dynamic construction of the serialization...
order by delaying it until validation. At that
tomant, more information on dependencies among
transactions is available than in continuous
methods. Nevertheless, previously described
methods [Kung 81], [Visont 82], [Schlagter 81]
impose that this order should be identical to
the chronological order of validations.

In this study, we propose and prove a
new certification CCM which, by using
intervals of timestamps, allows construction
of the serialization order which may differ
from the chronological order of validations.
Moreover, the gradual construction of the
serialization order makes detecting
non-serializable actions possible without
waiting until the transaction's validation.
This characteristic connects our method to
continuous CCMs and allows their comparison.

More precisely, the advantages and
originalities of our method compared to known
CCMs are the following:

1) It allows a chronological order of
validations which differs from the
serialization order thus increasing the number
of rejections or waitings.
The multiversions TO CCMs [Reid 78]
which also do not impose identity
between these two orders request a lot
more information (versions and
timestamps) about transactions' history
than our method.

2) It allows an "old" transaction to use, in
some cases, results of "younger" ones.
This property which requires dynamical
construction of the serialization order
without using chronological starting
time of transactions is also achieved by
2PL CCMs. Intervals of timestamps permit
this property to be obtained in our
method.

3) It allows favoring a particular class of
transactions (reading or writing ones, for
instance).
Such strategies may be implemented by
proper choice of the final timestamp
inside the interval of timestamps
associated to a given transaction.

4) It is fully integrated into a distributed
validation protocol.

Our study is organized as follows.

In section 2, we present the notion of
conflicts and the notion of dependency graph
which is the basis of formal proof of our
method. This graph maintains two types of
dependencies: effective ones and potential
ones. It allows classifying various CCMs as
continuous or optimistic (either "backward"
or "forward") according to their serialization
criterion and shedding some light on their
limitations.

In section 3, the principle and proof of
an original certification CCM using intervals
of timestamps are described.

Section 4 specifies the implementation
in a distributed environment and details the
certification protocol used, which is also
applicable to other optimistic CCMs.

2. CONFLICTS AND DEPENDENCY GRAPH

Conflicts and dependencies

The life of a transaction is divided
into several sequential steps:
(1) a step when reads (R) and
prewrites (P) of
objects occur in the transaction's workspace,
(2) a certification step present only in
optimistic CCMs, checking whether all
operations of a transaction are serializable,
(3) possibly a validation step, only present
when the transaction is serializable, whose
effect is to turn on definitively, in an
atomic manner, the prewritings of a
transaction.

Two transactions conflict if one tries
to prewrite (resp. read) an object already
read or prewritten (resp. prewritten) by the
other. Depending on the nature and
chronological order of the operations, PP, RP
and PR conflicts are distinguished.

A conflict between T1 and T2 induces a
constraint on the serialization order of T1
and T2 which can be translated into a
dependency taking one of the following two
forms:

a) an effective dependency (T1→T2)
which means that T1 precedes T2 in the
serialization order;
b) a potential dependency (T1→T2)
which means that the order is not yet
determined but will be determined at
last when one of the transactions
validates.

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Table 1 summarizes all possibilities for setting of a dependency - assuming that the operation of $T_1$ precedes chronologically that of $T_2$ - according to the nature of conflict and whether $T_1$ is validated (then noted $T_1^\times$) or not (then called a living transaction).

<table>
<thead>
<tr>
<th>Type of the conflict</th>
<th>Nature of the dependency when the conflict occurs depending whether $T_1$ is validated or living</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T_1 \rightarrow T_2$</td>
<td>$T_1 \rightarrow T_2$</td>
</tr>
<tr>
<td>$T_1 \rightarrow T_2$</td>
<td>Either $T_1 \rightarrow T_2$ or $T_1 \rightarrow T_1$ and $T_2$'s writing ignored: Thomas' Rule</td>
</tr>
<tr>
<td>$T_1 \rightarrow T_2$</td>
<td>Either $T_1 \rightarrow T_2$ and delayed reading or $T_2 \rightarrow T_1$ and immediate reading</td>
</tr>
</tbody>
</table>

The dependency graph

The execution of a set of transactions may be represented by a dependency graph $G$ whose nodes are transactions and edges are dependencies induced by their conflicts. $G$ changes when a conflict arises or when a transaction is rejected or validated. In particular, validation of a transaction $T$ transforms its potential dependencies $T \rightarrow T'$ into effective ones either of the form $T \rightarrow T'$ or of the form $T \rightarrow T'$ when Thomas' rule [Thomas 79] has been chosen to be applied which means ignoring the writes of $T'$.

It has been proved [Papadimitriou 79] that a circuit of effective dependencies in $G$ prevents all transactions involved in that circuit to be serialized (i.e. to be equivalent to a serial execution of the same transactions).

Let us note that, as long as a transaction is not validated, the effective and potential dependencies it has generated translate actions whose effects have not yet been registered into the base. Conversely, since a validation is irreversible, it is necessary that all validated transactions be serializable, i.e. that no circuit exists among them. In order to obtain serialization of transactions, a solution is to reject a living transaction as soon as the setting of one of its dependencies leads to a circuit in $G$.

In order to show limitations of the various known CCMs, it is useful to distinguish the following subgraphs:
- $G^\times$, the validated graph, restricted to all validated transactions with their dependencies;
- $G_T^\times$, the selfish graph of $T$, restricted to all validated transactions and to the living transaction $T$ with their dependencies;
- $G^\times$, the living graph, restricted to all living transactions with their dependencies.

A total order among transactions which is compatible with the partial order defined by $G^\times$ is called a serialization order.

All CCMs apply a serialization criterion to keep $G^\times$ circuitless. In fact, depending on methods used, one or more preceding subgraphs are privileged. However, no method implements any graph to determine the serialization order. Indeed in a distributed environment exact view of the graph would be difficult to obtain on each site. Moreover it would not be compatible with a satisfying level of parallelism. Only one optimistic CCM relying on a centralized management of $G$ in a local broadcast network has been proposed so far [Dewitt 80].

Continuous control and the dependency graph

Continuous CCMs are characterized by the fact that no checking upon dependencies is necessary at validation time. That is why they check when reading or prewriting, the dependencies’ setup in order to ensure that $G_T^\times$ is circuitless for all living transactions $T$ and stays that way, whatever transaction is validating. They do so by forcing potential dependencies to be converted into effective ones in case of a PP conflict. In such a case validation will not change any dependency. This advantage is paid by more rejections or waits for transactions.

In 2PL methods [Rosenkrantz 78], [Eswaran 76], [Traiger 82] the chronological order of operations induces dependency when a conflict occurs: if the operation of $T_1$ precedes chronologically that of $T_2$, the dependency $T_1 \rightarrow T_2$ is set. If $T_1$ is already validated the dependency corresponds to Table 1 (when Thomas’ rule is never applied).
In case of conflict between living transactions, $T_2$ is then blocked (sometimes uselessly) until $T_1$ is validated in order to force the dependency $T_1 \rightarrow T_2$: parallelism is thus decreased. In these methods the serialization order corresponds to the chronological validations' order. The possibility of a deadlock, characterized by a circuit in $G^*$, is another drawback of these methods.

In TO CCMs [Bernstein 81] the order of the timestamps associated to transactions at their birth defines an "a priori" serialization order. If, when a conflict occurs, the effective dependency it generates does not correspond to the timestamps' order, the transaction which triggers the conflict is rejected. In case of a PR conflict between living transactions, the dependency chosen is that of the timestamps' order, imposing validations to follow this order (the serialization one). This is done by making a transaction wait if it wants to validate earlier than other ones which precede it in the serialization order. The TO CCMs insure that $G$ is always circuitless. A variant method, the multiversions TO [Reed 78] allows accepting reads and under certain conditions prewrites (and thus validation) even when their chronological order does not respect the order of timestamps at the high price of multiple timestamped versions of the same object. The major drawback of TO CCMs is setting "a priori" dependencies before a conflict occurs thus inducing useless rejections. Moreover, the more the timestamps' order is far from the real chronological order of the transactions' birth, the more rejections are generated. This can be avoided by resynchronizing timestamps' generators [Lamport 78] by inter-site messages. At last, transactions may suffer from starvation if repeated rejections occur. An improvement of TO CCMs consists in waiting for the transaction's first conflict before giving it a timestamp compatible with the induced dependency [Bayer 82]. This postpones the previous drawback to the second conflict when the timestamp is defined: this may induce a dependency between this transaction and those which are not and will never be in conflict with it.

Control by certification and dependency graph

Many strategies are possible depending whether certification of a transaction $T$ is considered in $G$, $G^*$ or $G^*$. Nevertheless in all known CCMs except ours, the serialization order corresponds to chronological order of validations.

In a certification strategy with $G^*$, concurrency control uses the validated transactions' history. A transaction $T$ is certified successfully if $G^*$ is circuitless. For that reason, such a method is called "backward control". The method described in [Kung 81], suggested for a centralized system but which may be applied as well in DDBs, illustrates this type of control. During the certification of $T$, the conflicts it has had with all validated transactions $T_i$ are checked to be of the form $T_i \rightarrow T$. Since PP conflicts follow validations' order (i.e. serialization order) they are ignored as well as conflicts of the type $T_i \rightarrow T$. In case of a PR conflict between $T_i$ (which prewrites) and $T$ (which reads) dependency's direction changes depending whether the read of $T$ precedes chronologically $(T_i \rightarrow T)$ or follows $(T \rightarrow T_i)$ the validation of $T_i$. Since the method does not distinguish between the relative order of reads and validations, it forbids $T \rightarrow T_i^*$ and thus it also forbids $T_i \rightarrow T$ which might be valid. The serialization criterion of $T$ is:

$$\text{Owrite}(T_i) \cap \text{Oread}(T) = \emptyset, \text{for all } T_i$$

where $\text{Oread}(T)$ and $\text{Owrite}(T)$ are the sets of objects respectively read and prewritten by $T$.

Another proposal [Lausen 82] aims at forbidding only dependencies of the type $T \rightarrow T_i^*$ by timestamping the reads relatively to the validations.

A certification strategy with $G$ allows more freedom because not only validated transactions are considered but also living ones under the angle of their future validations. In order to do so, all circuits in $G$ which contain $T$ are looked for when $T$ certifies. If no circuit is found, $T$ may be certified, otherwise the circuits must be eliminated by either:
i) rejecting T;
ii) rejecting another living transaction in each of the circuits for instance in order to minimize future rejections;
iii) in the special case when each circuit contains a potential dependency T→T' which has been translated into T→T' - making T wait until the certification of T' which will invert the dependencies, or certifying T using Thomas' rule for T' (giving T→T').

So far no method illustrates this type of strategy.

In a certification strategy with G^+, control does not use the history of validated transactions but considers only living transactions. It is therefore called a "forward control" [Haerder 82]. If, during the certification of T there are T_i→T dependencies (corresponding to RP conflicts) either all transactions which induce such dependencies are rejected or T is made to wait until T_i is validated or T is rejected. Here the serialization criterion is:

\[ \text{Owriteset}(T) \cap \text{Oreadset}(T_i) = \emptyset, \text{ for all } T_i. \]

The method described in [Schlageter 81] achieves this type of forward control in order to favor transactions which read, by delaying the validations of writing transactions which conflict with them. The transactions which read and write are serialized using a backward control.

Generally no previously described CCM by certification allows T→T_i^* dependencies: the major drawback is that it induces either waits (by delaying validations) or rejections (if validations must be immediate). At last, attention must be drawn to the fact that all CCMs by certification must process transactions' certifications in the same order on all sites in a distributed system. Indeed all sites must make the same decision based on the same sets of living transactions (i.e. G^+) or validated ones (i.e. G^*).

3. CERTIFICATION BY INTERVALS OF TIMESTAMPS

Principle of the method

The certification method we present uses a backward control: the serialization criterion for T must avoid any circuit in G^* T.

A summary of the dependencies in the preceding subgraphs is obtained by:
- timestamps expressing dependencies in G^*,
- intervals of timestamps summarizing dependencies in G^*_T,
- sets of objects translating dependencies in G^*.

The use of each mechanism is precised by the following.

**Timestamps**: to each validated transaction T_i^* is associated a timestamp t_i given at certification time such that:

**Property P1.** The order induced by timestamps values is compatible with the partial order of G^*.

**Intervals of timestamps**: to each living transaction T and for each object x that it has used (read or prewritten) is associated an interval of timestamps I(T,x)(1). The bounds of this interval express the strongest constraints between T and validated transactions which have accessed to x and must respectively precede or follow T.

More precisely, if we denote L(T,x) and U(T,x) respectively the lower bound and the upper bound of I(T,x), the following must hold:

**Property P2.** For each living transaction T and for each object x it has used, I(T,x) is compatible with the timestamps of all validated transactions which have also used x. This means that:

\[ \forall T \text{ living transaction, } \forall x \text{ object used by } T, \forall T_i^* \text{ validated transaction having used } x, \]

either T_i^*→T and then t_i < L(T,x) or T→T_i^* and then U(T,x) < t_i

Notice that intervals of timestamps allow keeping track of T→T_i^* dependencies. Thus it will be possible for a transaction T which precedes some validated ones in the serialization order to be certified and validated after them.

Grouping all constraints upon T can be obtained by:

\[ I(T) = \bigcap_{x \in X} I(T,x) \]

X being the set of objects used by T.

(1) In practice, only one interval per site S, I(T,S), may be used.

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Proposition 1. Any living transaction \( T \) which introduces a circuit in \( G^*_T \) verifies \( I(T) = \emptyset \).

Proof: consider a transaction \( T \) which introduces such a circuit in \( G^*_T \). In this circuit, let us call:
- \( T_f \) the transaction which follows \( T \), by one object by which the dependency cores, and
- \( T_p \) the transaction which precedes \( T \), by one object by which the dependency cores (we may have \( f = p \)).

This circuit induces the following relations:

\[
\begin{align*}
T_f & \rightarrow T_p \\
T_p & \leftarrow T_f \\
T & \leftarrow T_f \leftarrow T_p
\end{align*}
\]

From Pl, we have: \( T_f \leftarrow T_p \) if \( t_f \leq t_p \) and \( T_p \leftarrow T_f \) if \( t_p \leq t_f \).

Since \( I(T) = \bigcap_i X(T_i, x) \), we have:
- \( Vx \in X \) \( LI(T_i, x) \leq LI(T) \) and \( UI(T_i, x) \geq UI(T) \)

We finally have:
- \( LI(T) > LI(T_i, y) \Rightarrow t_i > t_p \Rightarrow UI(T_i, x) \geq UI(T) \)

thus: \( LI(T) > UI(T) \) if \( I(T) = \emptyset \). \( \square \)

Sets of objects: to each living transaction \( T \) are associated the set of objects it has read (\text{Readset}) and the set of objects it has prewritten (\text{Writset}). As a result, between two living transactions \( T \) and \( T' \):

a) effective dependency \( T \rightarrow T' \) is equivalent to:

\text{Readset}(T) \cap \text{Writset}(T') \neq \emptyset

b) potential dependency \( T \rightarrow T' \) is equivalent to:

\text{Writset}(T) \cap \text{Writset}(T') \neq \emptyset

The principle of the method is to keep properties Pl and P2 true through all actions read, prewrite and certify:

- when \( T \) reads or prewrites \( x \), the interval \( I(T, x) \) must be updated according to property P2;
- when \( T \) asks for its certification, \( I(T) \) must be computed according to its definition. Then if \( I(T) \neq \emptyset \), \( T \) is certified, otherwise \( T \) is rejected.

Moreover when \( T \) is certified, \( G^* \) is modified and therefore so are \( G^*_T \), for all other living transactions \( T' \). The modifications are made by:

- choosing a timestamp for \( T \) which keeps on property Pl.
- adjusting the interval \( I(T', x) \) of all transactions \( T' \) which have been in conflict with \( T \), on any object \( x \) used by \( T \).

The following proposition shows how a timestamp may be associated to a transaction:

Proposition 2. If a transaction \( T \), with \( I(T) \neq \emptyset \), asks for certification any \( t \in I(T) \) will verify property Pl.

Proof: \( I(T) \) denotes the strongest constraints between \( T \) and the validated transactions. More precisely:

- \( \forall t_k \) such that \( T \rightarrow T_k \) \( \bigcup UI(T_i) < t_k \) and \( \forall t_f \) such that \( T \leftarrow T_f \) \( \bigcup LI(T_i) > t_f \)

Thus any \( t \in I(T) \) (i.e. \( LI(T) < t < UI(T) \)) will be compatible with the dependencies in \( G^*_T \).

In 4, we shall show that the choice of \( t = LI(T) \) (or \( UI(T) \)) has a definite effect on the future of some living transactions.

When the timestamp \( t \) for transaction \( T \) is chosen, adjustment of all intervals \( I(T', x) \) of the living transactions \( T' \) will be done according to the type of conflicts between \( T \) and \( T' \) on \( x \). Let us recall that these dependencies are recorded by means of sets of objects. The adjustment will take the forms:

- if \( T \rightarrow T' \) then \( t \) is the right truncation point for \( I(T', x) \);
- if \( T \leftarrow T' \) then \( t \) is the left truncation point for \( I(T', x) \);
- if \( T \rightarrow T' \) two translations are possible: either \( T \rightarrow T' \) with appropriate adjustment of \( I(T', x) \) or \( T \leftarrow T' \) with appropriate adjustment of \( I(T', x) \) and ignoring the writing of \( T' \) at validation time (Thomas' rule).

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In order to make the method useful in practice, it is necessary to "forget" validated transactions. This is done, as in TO methods, by timestamping objects: to each object are associated the highest timestamps (noted respectively $R(x)$ and $W(x)$) of the validated transactions which have read or prewritten $x$. With these timestamps, the actions read and prewrite may use proposition 3 to keep on property P2.

**Proposition 3.** When a transaction $T$ reads [resp. prewrites] an object $x$, fixing $LI(T,x) > W(x)$ [resp. $> \max(R(x), W(x))$] will respect the dependencies with the validated transactions $T_k^*$ under the form $T_k^* \rightarrow T$.

**Proof:** When a transaction $T$ reads $x$, it conflicts with all validated transactions $T_k^*$ having prewritten $x$. ($T_k^* \rightarrow T$)

Since for all $T_k^*$, $t_k < W(x)$ and since we set $W(x) < LI(T,x)$ we have $t_k < UI(T,x)$.

Similarly when a transaction $T$ prewrites $x$, it conflicts with all validated transactions $T_j^*$ having read or prewritten $x$. ($T_j^* \rightarrow T$ or $T_j^* \rightarrow T$).

Since for all $T_j^*$, $t_j \leq \max(W(x), R(x))$ and since we set $\max(W(x), R(x)) < LI(T,x)$ we also have $t_j < LI(T,x)$.

Thus during a read or prewrite operation on an object $x$ by a transaction $T$, only $T_k^* \rightarrow T$ dependencies between $T$ and validated transactions $T_k^*$ in conflict with $T$ are set up (Thomas' rule will never be applied in such cases).

4. IMPLEMENTATION IN A DISTRIBUTED SYSTEM

Data structures local to each site

$I(T)$ which retains the strongest constraints between $T$ and validated transactions might be computed upon any partition of the set of objects, since the intersection of these intervals would give the same result as the intersection of $I(T,x)$ on all objects $x$ accessed by $T$. Partition by site seems particularly attractive in a distributed system.

For each living transaction $T$ which has accessed to the set $X_i$ of objects on the site $S_i$, this site manages the interval $I(T, S_i)$:

$$I(T, S_i) = \bigcap_{x \in X_i} I(T, x).$$

$I(T, S_i)$ is created when $T$ makes its first access to an object on site $S_i$, and will be locally updated by site $S_i$ either during further reads and prewrites of the transaction $T$ on objects located on $S_i$ or independently of $T$ during adjustment following certification of a transaction $T'$ having been in conflict with $T$ on some objects of site $S_i$.

All effective dependencies due to conflicts between $T$ and validated transactions on all sites are expressed by:

$$\bigcap_{s_i \in S_i} I(T, S_i) = \bigcap_{x \in X_i} I(T, x) = I(T).$$

In order to make the adjustment mentioned hereabove, each site $S_i$ also manages the sets $\text{Oreads}(T, S_i)$ and $\text{Owrites}(T, S_i)$ which are respectively the set of objects read by $T$ on $S_i$ and the set of objects prewritten by $T$ on $S_i$. Each site $S_i$ also maintains the set $\text{Tliving}(S_i)$ of all living transactions known by it.

**Access to the objects**

In order to detect as soon as possible that an operation requested by a transaction is not serializable - and so have a kind of continuous control - to each transaction $T$ is associated its current interval $I_c(T)$. At the beginning of $T$, $I_c(T)$ is initialized as $[0, \infty]$ (the whole set of allowed timestamps). $I_c(T)$ is transmitted during each read or prewrite made by $T$ to the various sites accessed by $T$. These sites modify the interval according to dependency induced by the operation and send it back to the transaction $T$. Thus each site gets a more precise view on the dependencies involving $T$ which have been set on other sites.

Notice that now $I(T, S_i)$ not only carries information about the dependencies set on site $S_i$ but also has some knowledge of the preceding constraints put on $I(T)$. The final intersection of all $I(T, S_i)$ will still give the same $I(T)$ since although some constraints will be counted many times, the intersection will not be affected.

The advantage of using $I_c(T)$ which can be considered as an approximation of $I(T)$, is that it conveys more information on the constraints put on $T$, and therefore may signal rapidly that a transaction $T$ must be rejected.
when \( T_1(T) = 0 \). Taking this shortcut into account, the semantics of operations 
\[
\text{read}(x, T, I_c(T)) \quad \text{and} \quad \text{prwrite}(x, T, I_c(T))
\]
which preserves proposition 3 are given below. Each algorithm is executed on the site \( S_i \) of the object \( x \). For these algorithms it is assumed that the intervals contain only integers.

**Algorithm 1:**

\[
\text{read}(x, T, I_c(T))
\]

- If \( T \in \text{livingset}(S_i) \), then \( I_c(T) := I_c(T) \cap I(T) \),
- Else \( T \in \text{livingset}(S_i) := \text{livingset}(S_i) \cup \{ T \} \),

\[
\text{I}_c(T) := \text{I}_c(T) \cap \text{I}(x) + 1.0 \cdot \text{I}(x);
\]

\[
\text{r} = \text{send}(x, T, I_c(T));
\]

\[
\text{prwrite}(x, T, I_c(T))
\]

- If \( T \in \text{livingset}(S_i) \), then \( I_c(T) := I_c(T) \cap I(T) \),
- Else \( T \in \text{livingset}(S_i) := \text{livingset}(S_i) \cup \{ T \} \),

\[
\text{I}_c(T) := \text{I}_c(T) \cap \text{I}(x) + 1.0 \cdot \text{I}(x);
\]

\[
\text{r} = \text{send}(x, T, I_c(T));
\]

**Local adjustment of the intervals**

In order to fulfill property P2, certification of a transaction \( T \) implies adjustment of intervals of living transactions \( T' \) in conflict with \( T \), on all sites \( S_i \) where \( T \) is known as having accessed to some objects. In order to speed up the search for all transactions \( T' \) in conflict with \( T \), each site associates to each object \( x \), the sets \( Treadset(x) \) and \( Tprwritset(x) \) of living transactions which have respectively read or prwritten \( x \).

The semantics of the procedure \( \text{adjust}(T, t) \) which preserves property P2 through the certification of \( T \) with timestamp \( t \), is described below. It must be executed on all sites \( S_i \) accessed by \( T \).

We have included in this procedure, by means of the procedure \( \text{swap} \), the validation phase of \( T \) which corresponds to the copy of the new values of objects prwritten by \( T \) into the part of base managed by \( S_i \).

On each site the adjustment of intervals following the certification of \( T \) must not interfere with processing of reads or prwrites issued by other transactions \( T' \):

**Procedure adjust**

\[
\text{adjust}(T, t)
\]

- For \( x \) COreadset \((T, S_i) \) do
- For \( T' \in Treadset(x) \) do
- \( I(T', S_i) := I(T', S_i) \cap (t - 1, +\infty) \);
- \( r(x) := \text{send}(x, t, r(x)); \)
- For \( T' \in Tprwritset(x) \) do
- \( I(T', S_i) := I(T', S_i) \cap (t, +\infty) \);
- \( r(x) := \text{send}(x, t, r(x)); \)
- \( \text{send}(x, t, r(x)); \)

**Remark.** This critical section may be shortened by decomposing the procedure in many critical sections in order to exclude selectively the processing of reads and of prwrites depending on the part of the adjustment which is made.

The protocol of distributed certification

The certification of a transaction \( T \) is triggered at the end of its read/prwrite phase by the broadcasting of the message \( \text{certify}(T, I_c(T)) \) to all sites managing objects used by \( T \). The processing of this message on each site starts the certification protocol. Let us notice that it is necessary to insure that all concerned sites process the certifications in the same order in case of simultaneous ends of several conflicting transactions.

When communication between sites uses an unique broadcasting medium (Ethernet for instance) reception order of messages is the same on all sites. In this case, it is sufficient that certification messages are processed in the order of their reception to fulfill the previous condition. On the other hand, when the sites are linked together by a general network, the global ordering of certification messages must be done using a special mechanism like synchronization by timestamps \( \{\text{Lamport 78}\} \) or by circulating token \( \{\text{Lalann 78}\} \) not described here.

In the proposed protocol, no site plays a privileged role. On each site \( S_i \) concerned by the certification of \( T \), protocol consists in 3 phases:
- a proposal phase when $S_i$ broadcasts its $I(T, S_i)$ to all other sites and waits for their proposals.
- a choice phase when $S_i$ computes $I(T) = \bigcap_j I(T, S_j)$ which will thus be the same on all sites, and then applies the serialization criterion (cf. proposition 1): if $I(T) = \emptyset$ then $T$ is rejected, otherwise a timestamp value $t_T$ is chosen in $I(T)$ to be associated to $T$ (cf. proposition 2). The protocol must ensure that all the sites will choose the same value $t_T$. Choice of $t_T = UI(T)$ fulfills this condition, for instance. Other choices will be discussed later.
- an adjustment phase for the intervals of other living transactions $T'$ which includes also the validation of $T$.

![Diagram of the certification process]

**Figures.** The different stages of the certification.

Between the instants (1) and (4) the site $S_i$ may process read and prewrite messages issued by other transactions but no other certification message. An optimization would allow the simultaneous processing of transactions' certifications which did not conflict between them on a given site.

The processing of the message $\text{certify}(T, I_c(T))$ received by site $S_i$ is described below. Each site $S_i$ is assumed to know all the other ones involved in certification of $T$. The critical section is bracketed with '<' and '>'.

\[
\text{certify}(T, I_c(T)) = \begin{cases} 
(I(T, S_i) = I(T) \cap I(T, S_i)); & \text{broadcast-message}(\text{propose}(T, I(T, S_i))); \\
\text{wait for the proposals from } S_1, S_2, \ldots, S_n; & \text{if all proposals have been received} \\
I(T) = \emptyset & \text{else (choose } t_T); \\
\text{then reject } T & \langle \text{adjust}(t_T) \rangle). 
\end{cases}
\]

This protocol may be improved by not letting wait a site which has detected that $I(T, S_i) = \emptyset$, i.e., $T$ must be rejected. Later on, all other sites will take the same decision in their choice phase.

**Choice of the certification timestamp**

During the certification of $T$, each site $S_i$ must apply an identical strategy for choosing $t_T$ in $I(T)$, for instance $t_T = LI(T)$. This choice may have identifiable effects on other living transactions $T'$ in conflict with $T$. If we note $T'_R$ those which have only read objects and $T'_{RP}$ those which have prewritten, the value $t_T$ will truncate the intervals of $T'_{RP}$ on the left and those of $T'_R$ on the right.

Choosing $t_T = LI(T)$ leaves both the greatest interval for each $T'_{RP}$ and the smallest for each $T'_R$. This tends to decrease risk of rejection for transactions $T'_{RP}$ and simultaneously increase that for $T'_R$. Choosing $t_T = UI(T)$ would have the reverse effect.

Such a definite effect can be considered as a forward control. With more information about living transactions, other choices could be devised for minimizing the number of rejections for instance.

**Starvation**

The method may be adapted to avoid starvation. A transaction which wants to avoid starvation must broadcast to all sites a **prioritary-certify** message at start time. On each site, processing of this message will start a protection phase ending with the certification of $T$. During this protection phase all certifications -prioritary or not - will be delayed; the reads and prewrites will be done as usual.

In other words, the method forces all other transactions to be certified after the complete execution of $T$. Therefore only dependencies of type $T_k \rightarrow^* T$ will be set during $T'$s life, since dependencies of type $T \rightarrow^* T_k$ are only possible if $T_k$ is certified after the beginning of $T$, which has been avoided during the protection phase. Consequently no circuit will occur in $G^*_T$ and $T$ will be certified successfully.

5. CONCLUSION

By classifying various CCMs according to the type of dependencies they take into account, we have been able to make their limitations clear. Such an approach shows that there exists a continuum of methods between continuous control and control by...
In our method, use of intervals of timestamps allows us to summarize dependencies in $G^{*}$ without washing out those of type $T_{1} - T_{2}$. It becomes then possible to accept a chronological order of certifications different from the serialization order, which avoids arbitrary rejections.

Since the intervals of timestamps are broken into locally managed intervals on each site, without needing any synchronization messages before the certification step, our method is particularly well suited to a distributed environment.

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